# R20A2110 AIRCRAFT STRUCTURES

## **COURSE FILE**

## **III B. Tech I Semester**

## (2022-2023)

## **Prepared By**

## Dr. Ajith Raj R, Associate Professor

## **Department of Aeronautical Engineering**



# MALLA REDDY COLLEGE OF ENGINEERING & TECHNOLOGY

## (Autonomous Institution – UGC, Govt. of India)

Affiliated to JNTU, Hyderabad, Approved by AICTE - Accredited by NBA & NAAC – 'A' Grade - ISO 9001:2015 Certified) Maisammaguda, Dhulapally (Post Via. Kompally), Secunderabad – 500100, Telangana State, India.

## **MRCET VISION**

- To become a model institution in the fields of Engineering, Technology and Management.
- To have a perfect synchronization of the ideologies of MRCET with challenging demands of International Pioneering Organizations.

## **MRCET MISSION**

To establish a pedestal for the integral innovation, team spirit, originality and competence in the students, expose them to face the global challenges and become pioneers of Indian vision of modern society.

## MRCET QUALITY POLICY.

- To pursue continual improvement of teaching learning process of Undergraduate and Post Graduate programs in Engineering & Management vigorously.
- To provide state of art infrastructure and expertise to impart the quality education.

## PROGRAM OUTCOMES (PO's)

#### Engineering Graduates will be able to:

- 1. **Engineering knowledge**: Apply the knowledge of mathematics, science, engineering fundamentals, and an engineering specialization to the solution of complex engineering problems.
- 2. **Problem analysis**: Identify, formulate, review research literature, and analyze complex engineering problems reaching substantiated conclusions using first principles of mathematics, natural sciences, and engineering sciences.
- 3. **Design / development of solutions**: Design solutions for complex engineering problems and design system components or processes that meet the specified needs with appropriate consideration for the public health and safety, and the cultural, societal, and environmental considerations.
- 4. **Conduct investigations of complex problems**: Use research-based knowledge and research methods including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions.
- 5. **Modern tool usage**: Create, select, and apply appropriate techniques, resources, and modern engineering and IT tools including prediction and modeling to complex engineering activities with an understanding of the limitations.
- 6. **The engineer and society**: Apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal and cultural issues and the consequent responsibilities relevant to the professional engineering practice.
- 7. Environment and sustainability: Understand the impact of the professional engineering solutions in societal and environmental contexts, and demonstrate the knowledge of, and need for sustainable development.
- 8. **Ethics**: Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice.
- 9. **Individual and team work**: Function effectively as an individual, and as a member or leader in diverse teams, and in multidisciplinary settings.
- 10. **Communication**: Communicate effectively on complex engineering activities with the engineering community and with society at large, such as, being able to comprehend and write effective reports and design documentation, make effective presentations, and give and receive clear instructions.
- 11. **Project management and finance**: Demonstrate knowledge and understanding of the engineering and management principles and apply these to one's own work, as a member and leader in a team, to manage projects and in multi disciplinary environments.
- 12. Life- long learning: Recognize the need for, and have the preparation and ability to engage in independent and life-long learning in the broadest context of technological change.

## DEPARTMENT OF AERONAUTICAL ENGINEERING VISION

Department of Aeronautical Engineering aims to be indispensable source in Aeronautical Engineering which has a zeal to provide the value driven platform for the students to acquire knowledge and empower themselves to shoulder higher responsibility in building a strong nation.

#### MISSION

The primary mission of the department is to promote engineering education and research. To strive consistently to provide quality education, keeping in pace with time and technology. Department passions to integrate the intellectual, spiritual, ethical and social development of the students for shaping them into dynamic engineers.

### **QUALITY POLICY STATEMENT**

Impart up-to-date knowledge to the students in Aeronautical area to make them quality engineers. Make the students experience the applications on quality equipment and tools. Provide systems, resources and training opportunities to achieve continuous improvement. Maintain global standards in education, training and services.

### **PROGRAM EDUCATIONAL OBJECTIVES – Aeronautical Engineering**

- PEO1 (PROFESSIONALISM & CITIZENSHIP): To create and sustain a community of learning in which students acquire knowledge and learn to apply it professionally with due consideration for ethical, ecological and economic issues.
- PEO2 (TECHNICAL ACCOMPLISHMENTS): To provide knowledge based services to satisfy the needs of society and the industry by providing hands on experience in various technologies in core field.
- 3. **PEO3 (INVENTION, INNOVATION AND CREATIVITY):** To make the students to design, experiment, analyze, and interpret in the core field with the help of other multi disciplinary concepts wherever applicable.
- 4. **PEO4 (PROFESSIONAL DEVELOPMENT):** To educate the students to disseminate research findings with good soft skills and become a successful entrepreneur.
- 5. **PEO5 (HUMAN RESOURCE DEVELOPMENT):** To graduate the students in building national capabilities in technology, education and research

## **PROGRAM SPECIFIC OUTCOMES – Aeronautical Engineering**

- 1. To mould students to become a professional with all necessary skills, personality and sound knowledge in basic and advance technological areas.
- To promote understanding of concepts and develop ability in design manufacture and maintenance of aircraft, aerospace vehicles and associated equipment and develop application capability of the concepts sciences to engineering design and processes.
- Understanding the current scenario in the field of aeronautics and acquire ability to apply knowledge of engineering, science and mathematics to design and conduct experiments in the field of Aeronautical Engineering.
- 4. To develop leadership skills in our students necessary to shape the social, intellectual, business and technical worlds.

## MALLA REDDY COLLEGE OF ENGINEERING AND TECHNOLOGY

## III Year B.Tech. ANE- I Sem

L/T/P/C 3/-/-/3

## (R20A2110) Aircraft Structures

### **OBJECTIVES:**

The course should enable the students to:

- 1. Familiarize with modern aircraft structures.
- 2. Investigate buckling of plates
- 3. Obtain knowledge on Strain Energy
- 4. Idealize a real aircraft structure
- 5. Analyze various structural components like wing and fuselage

## UNIT –I

### THEORY OF THIN PLATES AND THIN WALLED BEAMS

Analysis of thin rectangular plates subject to bending, distributed transverse load, combined bending and twisting, Wagner beam analysis.

## UNIT –II

### UNSYMMETRICAL BENDING

Unsymmetrical bending-resolution of bending moments - direct stress distribution, shear flow in open section beams, shear centre, Torsion of thin walled closed section- Bredth - Batho shear flow.

### UNIT-III

### STRUCTURAL IDEALIZATION AND LOADING DISCONTINUITIES IN THIN WALLED BEAMS

Structural idealization of different aircraft components, shear stress distribution at a built in end of aclosed section beam.

### UNIT-IV

### STRESS ANALYSIS OF AIRCRAFT COMPONENTS

**Wing and Fuselage** - Direct stress and shear flow distribution -Wing spars, tapered wing and fuselage frames.

## UNIT-V

### **ENERGY METHODS**

Strain Energy due to axial, bending and torsional loadings. Deflection in beams- Castigliano'stheorem **Text Books:** 

- 1. Aircraft structures for engineering students by T H G Megson
- 2. Strength of materials by Hibler.
- 3. Strength of materials by R.S.Khurmi.

## **Reference Books:**

- 1. David J. Peery "Aircraft Structures" McGraw Hill Book Company.
- 2. Argyris J.H. and Kelsey S.Energy theorems and structural analysis, Butter worths Scientific Publications 1960.

#### Malla Reddy College of Engineering and Technology (MRCET)

2.440.94 e Acrospose Vehicle Structures & Aircraft Vehicle Structures host spect Unil - 1 This place theory, Structural Enstability: Analysis of this rectangular plates subject to bending. Inisting distributed Gransverse Load, Combined bending and in plane Loading, local instability. Wagner beam analysis. Sheet of metal whose thickness is small but is Thin plates: Capable of resisting bending. Force when applied to an object tends to change : its motion or its shape. In Structural engineering we have well defined cross sections and house members have a longitudinal and a lateral aris. It vertice aris hatod and / longitudinal ans The force applied in the longitudinal and of the member would tend to elongate (Tensile Force) or ( compressive vorce ) of the nomber. Compress

A jorse applied in the lateras while a price of the to slice of the member (shear jorce) or Words. try to bend the member (Bending Motherit) The amount of elongation, Compression, or shearing is directly dependent on the magnitude of the force applied. The more is the force, more is the effect. But the Same à not the Case with rotation. The Same amount of force if applied. A a greater distance would produce greates rotati Moment of yore: Moment of poste is the product of force and the distance. Twisting moment: If the moment porce try to twist the member then we call it as twisting moment or tor Storp Bending mo menti If the moment of force tried to bend

the member, then we Call it bendirg-moment.

A Section

at i fast a strage

Assumptions:

1. Displacement of plate in the direction Parallel to 3-aris is small when compared ? with the thickness.

2. The sections are plane before bending remain plane after bending. 3. The middle plane of the plate dises not dejorm during bending and is there fore Called a neutral plane.

4. Take neutral plane as the reference plane.

Consider an element of the Plate of Side Sx, Sy and having a depth aqual to thickness t'. Some Eg Pr, By are radii of Curvature of neutral plane in x-z and y-z plane : Positive Curvature of the plate corresponds to the positive bending moment which produce displacement in the Positive direction of the 3 or downwood direction.

Let En, Ey be the Strain in the

t

x, xy directions respectively.  $\mathcal{E}_n = \frac{1}{E} \left( \sigma_x - v \sigma_y \right) - \mathbf{r}$  $E_y = \frac{1}{E} \left( \overline{o_y} - \sqrt{o_n} \right) - 2$ 

Thin Rectangular Plates Subjected to bending ( Mn ] +12. My Horat Jan c | t/2je lagante por damo) Maller & Land Same Sy and the the days it is seen built of the part Let Mn, My be the bending moments of intensity per wit length uniformly distributed along its edges. along its edges. Mn => Bending moment applied along the edges parallel to y-aris My => Bending moment applied along the edges parallel to n-anis Bending moments are positive when they produce compression at the upper surface and tension at lower surface of plate.

(1) + (1) =>

 $= 2\phi_{x} - 2\phi_{y} + \phi_{y} - 2\phi_{x}$ + E 3 Cy E <u>3</u> Pn  $E \Im \left( \frac{\partial}{\partial_{n}} + \frac{1}{\partial_{y}} \right) = \left( \frac{\partial}{\partial_{y}} - \frac{\partial}{\partial_{y}} \right)$  $E_{J}\left(\frac{v}{e_{n}}+\frac{1}{e_{y}}\right) = O_{J}\left(1-v^{2}\right)$  $\overline{O_{y}} = \frac{E_{y}}{1 - \gamma^{2}} \left( \frac{\overline{\gamma}}{e_{n}} + \frac{1}{e_{y}} \right)$ 

 $M^{*} \vec{\gamma} \times (3) \rightarrow 3 = \vec{\gamma} \cdot \vec{\sigma} \cdot \vec{\gamma} - \vec{\sigma} \cdot \vec{\sigma}$ 

(3) The Koy be the direct stress along rand directions.

W.K.T bending moment ign. is  $\frac{M}{I} = \frac{G}{Y} = \frac{E}{R}$  $\frac{\sigma}{E} = \frac{y}{R} \quad w \quad E = \frac{y}{R}$ from fig.  $\mathcal{E}_{n} = \frac{3}{\mathcal{C}_{n}} - 3$ Ey = 3 - (1) where Pn & Py be the radii By Py of Curvature in Neutral plane. sub. 3 in () & (  $\frac{1}{E}\left(\sigma_{n}-\sqrt{\sigma_{y}}\right)=\frac{3}{e_{n}}$ -6)  $\frac{\Im E}{\operatorname{Cn}} = \left( \operatorname{O_n} - \operatorname{VO_y} \right)$ 0 Sub Din (1)  $\frac{1}{E}\left(\frac{\sigma_{y}}{2}-\gamma\sigma_{x}\right)=\frac{\delta}{P_{y}}-\overline{\partial}$  $\frac{\partial E}{\partial y} = (\nabla y - V \nabla x)$ 8 7× () =)  $E \frac{\partial}{\partial x} = V \sigma_n - V \sigma_y$ - 9

$$= \frac{1}{\sqrt{3}} \frac{E}{(1-v^2)} \int_{-1}^{1} \frac{t^3}{8} + \frac{t^3}{8} \int_{-1}^{1} \frac{E}{8} \int_{-1}^{$$

W. K.T



 $\overline{\mathcal{D}} \text{ is the place wat regidity of the place }$   $\overline{\mathcal{D}} = \int \frac{E_{3}^{2}}{1 - \sqrt{2}} dz$   $-\frac{1}{\sqrt{2}} \int \frac{E_{3}}{1 - \sqrt{2}} dz$   $= \frac{E}{1 - \sqrt{2}} \int \frac{3^{2}}{\sqrt{3}} dz$   $= \frac{E}{1 - \sqrt{2}} \int \frac{3^{3}}{\sqrt{3}} dz$   $= \frac{E}{1 - \sqrt{2}} \int \frac{3^{3}}{\sqrt{3}} dz$   $= \frac{1 - \sqrt{2}}{\sqrt{3}} \int \frac{1}{\sqrt{3}} dz$ 

-ve Sign indicates large of another his above  
the place:  

$$M_{n} = -\frac{E t^{3}}{i^{2}(1-p^{2})} \left[ \frac{\partial w}{\partial x^{2}} + \frac{p}{\partial \frac{\partial w}{\partial y^{2}}} \right]$$

$$M_{y} = -\frac{E t^{2}}{i^{2}(1-p^{2})} \left[ \frac{\partial w}{\partial y^{2}} + \frac{p}{\partial x^{2}} \right]$$

Here our aim is to relate the twisting moment May to w.

Consider an element of plate. The Shear Stresses on a Ramina of the element at a distance 3 below the neutral plane.

Sy Sn 5/2 May = - / Iny 3dz In terms of Shew strain Dry and modules of rigidity G  $M_{ny} = -G \int_{ny}^{t/2} 3dz$ Shear Strain, Bry = <u>DV + Du</u> Dn <u>Dy</u> An element taken through the thickness of the Plate will Suffer equal votations equal to Dio x dio in 23 and 33 planes. Considering the rotation of such an element

Plates Subjected to Bending and . ansver SMANY In general, the bending moments applied to the Plate will not be in planes perpendiculas to its edges. Such bending moments, however may be resolved in the normal manner into tangential and perpendicular components. Mx and My are the perpendicular components. May and Myn are the tangential components. May is the twisting moment intensity in a vertical x plane posallel to yarris. Myr is the twisting moment intensity in a vertically Plane parallel to x arris. Since the twisting moments are tangendial moments or torque they are resisted by a System of human of a System of horizontal Shear Stress Iny. May = - Myn

$$M_{my} = \frac{Et^{3}}{I2(1+2)} \frac{\partial^{2}\omega}{\partial n \partial y}$$

$$X \neq he numbers & denomical by (1-2)$$

$$M_{my} = \frac{Et^{3}(1-2)}{I2(1+2)(1-2)} \frac{\partial^{2}\omega}{\partial n \partial y}$$

$$= \frac{Et^{3}(1-2)}{I2(1+2)(1-2)} \frac{\partial^{2}\omega}{\partial n \partial y}$$

$$M_{my} = \frac{Et^{3}(1-2)}{I2(1-2)} \frac{\partial^{2}\omega}{\partial n \partial y}$$

$$M_{my} = \frac{Et^{3}(1-2)}{I2(1-2)} \frac{\partial^{2}\omega}{\partial n \partial y}$$

$$M_{my} = D(1-2) \frac{\partial^{2}\omega}{\partial n \partial y}$$

in ng plane, the displacement 4 in the north of a point at a distance g below the neutral plane is

3

$$u = -\frac{\partial \omega}{\partial g \times} 3$$

$$v = -\frac{\partial \omega}{\partial g} 3$$

$$v = -\frac{\partial \omega}{\partial g} 3$$

$$\frac{\partial v}{\partial n} = -\frac{\partial z}{\partial n} \frac{\partial \omega}{\partial y} = -\frac{\partial z}{\partial n} \frac{\partial \omega}{\partial n} \frac{\partial z}{\partial y} = -\frac{\partial z}{\partial n} \frac{\partial z}{\partial n} \frac{\partial z}{\partial y} = -\frac{\partial z}{\partial n} \frac{\partial z}{\partial n} \frac{\partial z}{\partial n} \frac{\partial z}{\partial n} \frac{d z}{\partial y} = -\frac{d z}{\partial n} \frac{\partial \omega}{\partial n} \frac{z}{\partial x} \frac{z}{\partial y} \frac{d z}{\partial n} \frac{d z}{\partial x} = -\frac{d z}{\partial n} \frac{\partial \omega}{\partial n} \frac{z}{\partial x} \frac{z}{\partial y} \frac{z}{\partial n} \frac{d z}{\partial x} \frac{z}{\partial x} \frac{z}{\partial x} \frac{z}{\partial y} \frac{z}{\partial x} \frac$$

Thin plates Subjected to Transverse Load ; y 1 L 03 3 Sn  $M_{n} + \frac{\partial}{\partial x} M_{n} Sn$ MNO >My+ D Mny. Sn Qu+ D Qu'Sn My + J Qy + J Qy · Sy dr My Sy transverse load of intensity of per unit an A is applied. The plate is subjected to bending and twisting and in addition vertical Shear Jorns Que Q Per wit length on joces perpendicular to nky anis respectively.

equade the forces in 3 direction,  $\left(Q_{n}+\frac{\partial}{\partial x}Q_{n}\delta_{x}\right)\delta_{y}-Q_{n}\delta_{y}+\left(Q_{y}+\frac{\partial}{\partial y}Q_{y}\delta_{y}\right)$ - QySn + 9Sn Sy =0 Qysy + 2 Qu Susy - Qysy + Qysu + 2 Qy Su  $-Q_y \delta_n + q \delta_n \delta_y = 0$  $\frac{\partial}{\partial n} Q_n S_n S_y + \frac{\partial}{\partial y} Q_y S_n S_y + q S_x S_y = 0$ Moment about ty aris is  $\frac{\partial}{\partial y} M_{ny} - \frac{\partial}{\partial n} M_n + Q_n =$ 0 0 Moment about x aris is 3  $\frac{\partial}{\partial n}$  M<sub>ny</sub>  $-\frac{\partial}{\partial y}$  M<sub>y</sub> +  $\frac{\partial}{\partial y} = 0$  $Q_n = \frac{\partial}{\partial n} M_n - \frac{\partial}{\partial y} M_n$ Qy =  $\frac{\partial}{\partial y}$  My -  $\frac{\partial}{\partial n}$  Mny Sub the value of Que & Qy in (1) Dr DAN D May Suby t ∂ ∂y dy - ∂ Mny Sr Sy = -9 Srdy

 $-D\left[\frac{\partial^4\omega}{\partial x^4} + \frac{\partial^4\omega}{\partial x^2 \partial y^2} + \frac{\partial^4\omega}{\partial x^2 \partial y^2} + \frac{\partial^4\omega}{\partial x^2 \partial y^2}\right]$  $-2 p \frac{\partial^{2} \omega}{\partial x^{2} \partial y^{2}} + \frac{\partial^{2} \omega}{\partial y^{4}} + \frac{\partial^{2} \omega}{\partial x^{2} \partial y^{2}} = -\frac{1}{2}$  $-D \left[ \frac{\partial \omega}{\partial n^{2}} + 2^{2} \frac{\partial \omega}{\partial n^{2} \partial y^{2}} + 2 \frac{\partial^{4} \omega}{\partial n^{2} \partial y^{2}} - 2^{2} \frac{\partial^{4} \omega}{\partial n^{2} \partial y^{2}} \right]$  $+ \frac{\partial^4 \omega}{\partial y^4} = -2$  $\frac{\partial^{+}\omega}{\partial n^{+}} + \frac{\partial^{+}\omega}{\partial n^{2}\partial y^{2}} + \frac{\partial^{+}\omega}{\partial y^{+}} = \frac{q}{D}$  $\left(\frac{\partial^2 \omega}{\partial n^2} + \frac{\partial^2 \omega}{\partial y^2}\right) \left(\frac{\partial^2 \omega}{\partial n^2} + \frac{\partial^2 \omega}{\partial y^2}\right) = \frac{q}{D}$  $\left(\frac{\partial^2 \omega}{\partial x^2} + \frac{\partial^2 \omega}{\partial y^2}\right) = \frac{9}{D}$  $\left(\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}\right)^2 \omega = \frac{q}{D}$ 

$$\frac{\partial^{2} M_{n}}{\partial n^{2}} = -\frac{\partial^{2} M_{ny}}{\partial n \partial y} + \frac{\partial^{2} M_{y}}{\partial y^{2}} - \frac{\partial^{2} M_{n}}{\partial n \partial y}$$

$$= -9$$

$$\frac{\partial^{2} M_{n}}{\partial n^{2}} - \frac{\partial^{2} \partial^{2} M_{ny}}{\partial n \partial y} + \frac{\partial^{2} M_{y}}{\partial y^{2}} = -9$$

$$M_{n} = -D \left( \frac{\partial^{2} \omega}{\partial n^{2}} + \sqrt{\partial^{2} \omega}}{\partial y^{2}} \right)$$

$$M_{y} = -D \left( \frac{\partial^{2} \omega}{\partial n^{2}} + \sqrt{\partial^{2} \omega}}{\partial y^{2}} \right)$$

$$M_{y} = D \left( 1 - \sqrt{2} \right) \frac{\partial^{2} \omega}{\partial n \partial y}$$

$$Sub in (A)$$

$$\frac{\partial^{2}}{\partial n^{2}} \left[ -D \left( \frac{\partial^{2} \omega}{\partial n^{2}} + \sqrt{\partial^{2} \omega}}{\partial y^{2}} \right) \right]$$

$$+ -\frac{\partial^{2} \partial^{2}}{\partial n \partial y^{2}} \left[ -D \left( \frac{\partial^{2} \omega}{\partial y^{2}} + \sqrt{\partial^{2} \omega}}{\partial y^{2}} \right) \right]$$

$$= -9$$

Wagnes Beam (Diagonal Field Beam) or (Tension Field Beam)

\* The ability of the thin Sheet metal to Gerry an increasing load after it began to buckle - which in conventional structures was regarded as failure

\* The Spars of aircryt wing usually comprise an upper and a lower plange connected by thin Stiffners.

\* These webs are often of Such a thickness that they buckle under Shear Stresses.

\* When the web of the beam buckles under the action of internal diagonal compressive stresses produced by Shear, diagonal tension is only capable of supporting to web.

\* The beam Shown below has Concentrated plange areas having a depth of between the Centroids and vertical stippeners which are placed wijformy along the length of the beam It is assumed that the planges resist

the interval bending moment at any Section of the beam, While the used of Thickness t, resists the Vertical Shear force.



$$= \frac{\partial W}{dd \sin \alpha} \cos \alpha$$

$$= \frac{W \cos \alpha}{dd \sin \alpha} \cos \alpha$$

$$= \frac{W \cos \alpha}{dd \sin \alpha}$$
On the horizondal place Hc is an immediat  
line down,  
 $\Im = \frac{\partial W}{dd \tan \alpha}$ 
 $\Im = \frac{\partial V}{dd \tan \alpha}$ 
 $\Im = \frac{\partial V}{dd \tan \alpha}$ 
 $F = \frac{\partial V}{d \tan \alpha}$ 

.

$$= \frac{2}{td} \frac{2}{d \sin \alpha} \cos \frac{1}{d \cos \alpha}$$

$$= \frac{W \cos \alpha}{td \sin \alpha}$$

$$= \frac{W \cos \alpha}{td \sin \alpha}$$

$$\int_{J} = \frac{W}{td \tan \alpha}$$
On dhe horizondal plane He is an immaging fine drawn,  

$$\int_{J} = \frac{1}{d \tan \alpha}$$



$$F_{T} = \frac{W_{3}}{d} + \frac{G_{3} + d}{2}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W + d}{td \tan \alpha} \frac{1}{2}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha} + \frac{W}{td \tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha} + \frac{W}{td \tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} + \frac{W}{2\tan \alpha} + \frac{W}{\tan \alpha}$$

$$F_{T} = \frac{W_{3}}{d} - \frac{W}{2\tan \alpha}$$

.

$$P = \frac{1}{d} \frac{1}{d}$$

$$F = \frac{1}{d} \frac{1}{d}$$

$$F = \frac{1}{d}$$

The direct stress of Guses Compressive log in the work Vertical Stippours. : P= Jxtx4 b P = Wton & xtxb to P = Wb tan a Determination of forge forces.  $= \downarrow \leftarrow F_{\epsilon}$ T F 3 m The direct load in the glarges are found by considering a length 3 of the beam. On the plane mm there are direct and Sheer Stresses of, I arding in the Web together with F and FB taking momentum about the bottom plange,  $W_{z} = F_{t} \times d + (\sigma_{z} \times t \times d) d_{z} = 0$  $W_3 + G_3 \pm \frac{d^2}{d} = F_7 d$ 

Maximum bending moment occurs at  
a stippes and is given by  

$$M_{mon} = Wb^2 \tan \alpha$$
  
 $M_{mon} = Wb^2 \tan \alpha$   
 $1/2 d$   
 $M_{mon} = Wb^2 \tan \alpha$   
 $2 d d$   
 $4m_{mon} = Wb^2 \tan \alpha$   
 $2 d d$   
 $4m_{mon} = Wb^2 \tan \alpha$   
 $1 + bb$   
 $As$ 

Problem C A Wagner beam of length 1200mm fined as a · Cantilever is subjected to a tip load of 5 km. The depth of the beam is 400mm, and stillnes spacing the is 300mm. The cross section areas of Manges offered stilleners are 350 mm² and 300 mm² respectively. The elastic section modulus of each is 750 mm<sup>3</sup>, the thickness of web is 2 mm and the and moment of area of stifferer about glarge an aris in the plane of web is 2000mmt. Determine the marri stress in a plange and also Whether the Stifferers will buckle or not. 14 1 G. 60 E = 70,000 N/mm<sup>2</sup> N5KN 400 mm 300 mm 1200 mm 1+<u>tol</u> 2 Aj tant & 1+ tb As 1+ 2×400 2× 350 1+ 2 × 300 300  $ton^{t} \propto = 0.71 f$ 

$$\left( \tan^{\frac{2}{2}} \right)^{\frac{1}{2}} = 0.714$$

$$\tan^{\frac{2}{2}} = 0.845$$

$$(\tan^{\frac{2}{2}})^{\frac{2}{2}} = 0.845$$

$$\tan^{\frac{2}{2}} = 0.919$$

$$a^{\frac{2}{2}} = 4^{\frac{2}{2}} \cdot 6^{\frac{2}{3}}$$

$$\tan^{\frac{2}{3}} = 4^{\frac{2}{2}} \cdot 6^{\frac{2}{3}}$$

$$= 4^{\frac{2}{2}} \cdot 6^{\frac{2}{3}}$$

$$= 4^{\frac{2}{2}} \cdot 6^{\frac{2}{3}}$$

$$= 4^{\frac{2}{2}} \cdot 6^{\frac{2}{3}}$$

$$= 5^{\frac{2}{3}} \cdot 1200 + \frac{5}{2} \tan^{\frac{2}{3}} + \frac{17 \cdot 720}{350} \times 10^{\frac{3}{3}}$$

$$= 17 \cdot 720 \times 10^{\frac{3}{3}}$$

$$= \frac{17 \cdot 720 \times 10^{\frac{3}{3}}}{350}$$

$$= \frac{5 \times 10^{\frac{3}{2}} \times 300^{\frac{2}{3}} \tan^{\frac{2}{3}} (4^{\frac{2}{3}} \cdot 6)}{\frac{12 \times 400}{12 \times 400}}$$

$$= \frac{5 \times 10^{\frac{3}{2}} \times 300^{\frac{2}{3}} \tan^{\frac{2}{3}} (4^{\frac{2}{3}} \cdot 6)}{\frac{12 \times 400}{12 \times 400}}$$

$$= \frac{8 \cdot 6 \times 10^{\frac{1}{7}} N \text{ mm}}{750 \text{ mm}^{\frac{3}{3}}}$$

$$= 114 \cdot 875 N/\text{mm}^{\frac{3}{2}}$$

-

i.

: Total Stress in top plange = 114.67+50.6 = 165.475 N/mm<sup>2</sup>

2

$$P = \frac{\sqrt{6} \tan x}{d}$$
  
=  $5 \times 10^{3} \times 300 \times \tan 42.6$   
 $400$   
=  $3.448 \times 10^{3} N$   
=  $3.448 \times 10^{3} N$ 

we know ,

$$P_{er} = \frac{\pi^2 E I}{l_e^2} \qquad \text{when } b \ge 1.5 d$$

$$l_e = \frac{d}{\sqrt{4 - \frac{2b}{d}}}$$

when 
$$b > 1.5d$$
  
 $le = d$ 

$$i le = \frac{400}{\sqrt{4 - \frac{2 \times 300}{400}}}$$

$$\frac{400}{\sqrt{4-1.5}} = \frac{400}{\sqrt{2}}$$

 $\frac{0}{15} = 252.988$ 

16

 $\frac{1}{12} P_{cr} = \frac{TC^2 \times 70 \times 10^3 \times 2000}{(2.52 \cdot 988)^2}$   $P_{cr} = 21.57 \text{ KiN}$   $P < P_{cr} \therefore \text{ Safe}, \text{ TLe- stiffener will not buchle.}$ 

$$\therefore \tan^{4} \alpha = \frac{1 + \frac{ta}{2Af}}{\frac{1 + \frac{tb}{As}}{As}} = \frac{1 - 200}{200}$$

$$= \frac{1 + \frac{1 \cdot 5 \times 350}{2 \times 300}}{\frac{1 + \frac{1 \cdot 5 \times 300}{280}}{280}}$$

$$F = \frac{W_3}{d} + \frac{w}{2\tan \alpha}$$

$$= \frac{5 \times 1200}{400350} + \frac{5}{2 \tan 426}$$

2. A simply supported beam has a span of en and Carries a Central Concentrated load of 10 km. The glanges of the beam each have a cross sectional glanges of the beam each have a cross sectional west area of 300 mm<sup>2</sup>, while that of the vertical west Stifferers is 280 mm<sup>2</sup>. If the depth of the beam measured between the conteroids of area of the glarges is 350 mm and the stifferers are symmetrical arranged about the web and Spaced at 300 mm intervals, determine the manimum anial load in a flange and compressive load in the stiffener. It may be assumed that the beam web. of thickness 1.5 mm, is Gpable of resisting diagonal tension only.

t = 1.5 mm d = 350 mm b = 300 mm  $A_{j} = 300 \text{ mm}^{2}$   $A_{j} = 280 \text{ mm}^{2}$   $g = 280 \text{ mm}^{2}$   $g = 280 \text{ mm}^{2}$  g = 2.4 mCentral load = 10 km


3. A thin Square plate of side a and thickness t is simply supported along each edge, and has a slight initial curvature giving an initial deflected shape. Wo = SSIN The sin Thy My the plate is subjected to a uniform compressive Stress of in the x direction find an expression for the elastic deflection w normal to the plate Show also the deflection at mid poind of the plate can be presented in the form of a Southwell plat and illustrate your answer with Switable Shedch.

$$w_{1} = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} B_{mn} \sin \frac{m\pi\pi}{a} \sin n\pi \frac{\pi}{a}$$

$$w_{1} = \sum_{m=1}^{\infty} \sum_{n=1}^{\infty} B_{mn} N_{n} \frac{m\pi\pi}{a} \sin n\pi \frac{\pi}{a}$$

$$B_{mn} = \frac{A_{mn} N_{n}}{(\pi^{2}D/a^{2})\left[m + (n^{2}a^{2}/mb^{2})\right]^{2}} - N_{n}$$

$$hat m=n=1, a=b and N_{n} = \sigma\tau , A = S$$

$$B_{mn} = \frac{S\sigma\tau}{(\pi^{2}D/a^{2})\left[1 + (\frac{a^{2}}{a^{2}})\right]^{2}} - \sigma\tau$$

$$= \frac{S\sigma\tau}{(\pi^{2}D/a^{2})\left(1 + 1\right)^{2}} - \sigma\tau$$

$$w_{n} = num confluence in a direction of the form of satisfy the area in a direction of the form of satisfy the area in a direction of the form of the form$$

the deplection at certire of the plate
where $x = \frac{\alpha}{2}, y = \frac{\alpha}{2}, den$
$W_{c} = \frac{S \sigma t}{(4\pi^{2}D/a^{2}) - \sigma t} \qquad \frac{S in \pi x q}{2xq} \qquad \frac{S in \pi x q}{2xq}$
$\omega_{c} = \frac{S \sigma t}{\left(4 \overline{u}^{2} D / a^{2}\right) - \sigma t}  S \times 1 \times 1$
$w W_c = \frac{S\sigma t}{(4\pi^2) - \sigma t}$
when Ot -> 4TT D/2, W -> and Ot -> Ny up
the buckling load of the plate may be
horitten as
$W_{c} = \frac{S \sigma t}{N_{ncR} - \sigma t}$
5 St
Wn cr
I - Ot. Nncr
le theze a The graph an be drown for We against oft which will be a Straight for J slope Nuce and intercepts at S
Le. Southwell plot.

D. Alian Ry R Unit - I Aeso MR Car Unsymmetrical Bending Moment of Inertia The moment of a force also called the 1st moment of Good force about any point is the product of the force and the I' distance between them. If this 1st moment of force is again multiplied by the tr distance it is called the and moment of force. If instead of force, the area of the object is considered, then it is Called 2nd moment of area or moment of Irestia. Principal plane and Stress. The plane carrying the maximum normal Stress is called the major principal plane and the corresponding Stress is major principal stress The plane Guerring the minimum normal Stress is transmission of the minimum 1 at is known as minor principal plane and the corresponding. Strass is known as minor principal Stras.  $\sigma_1 = \left(\frac{\sigma_n + \sigma_2}{2}\right) + \sqrt{\left(\frac{\sigma_n - \sigma_2}{2}\right)^2 + Z_{ny}^2}$  $G_{2} = \left(\frac{\sigma_{n} + \sigma_{y}}{2}\right) \not\equiv -\left(\frac{\sigma_{n} - \sigma_{y}}{2}\right)^{3} + I_{ny}^{2}$ O, Oz are major & minor principal stress.

Principal moment of Inertia. If the two arres about which the product of inertia is found such that the produit of inertia becomes zero, the two areas are then called principal area. The moment of inertia about the Principal avis is Called the principal moment of inertia het us conside a 2D fig. where c.g is the Centre of growity, the elementary and will pass through e.g. let u.u and V-V be the principal arres. principal ares. u-u -> major principal anis v-v -> minor principal anis Fun -> manimum moment of inertia Pur - minimum moment of Instia  $\frac{\Gamma_{uu}}{2} = \frac{\Gamma_{uu} + \Gamma_{yy}}{2} + \sqrt{\left(\frac{\Gamma_{yy} - \Gamma_{nu}}{2}\right)^2 + \Gamma_{ny}}$ Que = <u>Innt Gyy</u> - <u>UGy</u> - <u>Inn</u> <u>2</u> d bocation of principal and <u>J</u>  $\tan 2\theta = \frac{2 \operatorname{Iny}}{\operatorname{Iyy} - \operatorname{Inn}} \xrightarrow{x}$ 

5 Direct Stress Distribution due to bending. 5mg x p(m) a 72 Jy cost Consider the Cross Section of beam as in fig. Let Mr. & My be the bending moment about some any of the cross Section. Let G be the Centroid of the Section. Then XX& YY be the Mulually I'r anis passing Section. Then XX& YY be the Newtral and is possing through the Centroid. Consider Newtral and is possing through the Centroid. Let P be a point at x and y distance juin du anis. a' be dhe distance betweens Neudral anis and point pri let of be the Stress By the beam is bend to a radiu of curvature about N.A. at this seek,  $\frac{\sigma}{E} = E$ w.k.  $\frac{M}{T} = \frac{\sigma}{a} = \frac{E}{r}$ where  $\xi = \frac{Q}{Y}$ pure bending, therefore The beam is Subjected 10 Joda = 0

$$Q = \pi \sin \alpha t \ y \cos \alpha \quad -\infty$$

$$S = \Theta \quad in \quad O$$

$$= \frac{E}{Y} \left( \pi \sin \alpha t \ y \cos \alpha \right)$$

$$W = \int O = \frac{E}{Y} \left( \pi \sin \alpha t \ y \cos \alpha \right)$$

$$M_{\pi} = \int O = y dA$$

$$M_{\pi} = \int J^{2} dA$$

$$F_{\pi} = \int J^{2} dA$$

$$F_{\pi} = \int \pi^{2} dA$$

$$G_{\pi} = \int \pi^{2} dA$$

$$M_{\pi} = \frac{E}{Y} \int (\pi \sin \alpha t \ y \cos \alpha) \ y dA$$

$$= \frac{E}{Y} \int \pi^{2} \sin \alpha dA t \frac{E}{Y} \int y^{2} \cos \alpha dA$$

$$M_{\pi} = \frac{E}{Y} \int (\pi \sin \alpha t \ y \cos \alpha) \ \pi dA$$

$$= \frac{E}{Y} \int (\pi \sin \alpha t \ y \cos \alpha) \ \pi dA$$

$$= \frac{E}{Y} \int (\pi \sin \alpha t \ y \cos \alpha) \ \pi dA$$

$$= \frac{E}{Y} \int (\pi \sin \alpha t \ y \cos \alpha) \ \pi dA$$

2.

 $M_{y} = \frac{E}{r} \left[ \frac{g_{yy}}{r} \sin \alpha + \frac{g_{ny}}{r} \cos \alpha \right]$  $\begin{bmatrix} M_{m} \\ M_{y} \end{bmatrix} = \frac{E}{Y} \begin{bmatrix} I_{my} & I_{mn} \\ I_{yy} & I_{my} \end{bmatrix} \begin{bmatrix} gin \alpha \\ cos \alpha \end{bmatrix}$  $\frac{E}{r} \begin{bmatrix} \sin \alpha \\ \cos \alpha \end{bmatrix} = \begin{bmatrix} M_n \\ M_y \end{bmatrix} \begin{bmatrix} T_{ny} & T_{ny} \\ T_{yy} & T_{ny} \end{bmatrix}$  $= \begin{bmatrix} Iny & -Inn \\ -Iyy & Iny \end{bmatrix} \begin{bmatrix} Mn \\ My \end{bmatrix}$ Fing & Fing Fing & Fing Fyy Fing = [any - Inn - Gyy - Iny] My Ing - Inn Lyy  $\frac{E}{r} \begin{bmatrix} \sin \alpha \\ \cos \alpha \end{bmatrix} = \frac{1}{\frac{2}{r_{wy}^{2}} - \frac{2}{r_{wy}} \frac{1}{r_{wy}} \begin{bmatrix} \frac{1}{r_{wy}} M_{w} - \frac{1}{r_{wy}} M_{y} \\ -\frac{1}{r_{wy}} M_{w} + \frac{1}{r_{wy}} M_{y} \end{bmatrix}$ 

$$\frac{E}{Y} \sin \alpha \cdot = \frac{\int ny \, M_N - \int x_N^m \, My}{\int y} \frac{1}{\int y_y^2 - \int n_N \int y} \frac{1}{\int y} \frac{1}{\int n_N^2 - \int n_N \int y} \frac{1}{\int y} \frac{1}{\int n_N \int y} \frac{1}{\int y} \frac{1}{\int y} \frac{1}{\int y} \frac{1}{\int y} \frac{1}{\int y} \frac{$$

at neutral anis, 0=0

 $\frac{\left[\begin{array}{c}M_{y} \widehat{I}_{nn} - M_{n} \widehat{I}_{ny}\right]}{\widehat{I}_{nn} \widehat{I}_{yy} - \widehat{I}_{ny}}\right]_{x} + \frac{\left[\begin{array}{c}M_{n} \widehat{I}_{yy} - M_{y} \widehat{I}_{ny}\right]}{\widehat{I}_{nn} \widehat{I}_{yy} - \widehat{I}_{ny}}\right]_{y} = 0$   $\frac{\left[\begin{array}{c}M_{n} \widehat{I}_{yy} - M_{y} \widehat{I}_{ny}\right]}{\widehat{I}_{nn} \widehat{I}_{yy} - \widehat{I}_{ny}}\right]_{y} = -\frac{\left[\begin{array}{c}M_{y} \widehat{I}_{nn} - M_{n} \widehat{I}_{ny}\right]}{\widehat{I}_{nn} \widehat{I}_{yy} - \widehat{I}_{ny}}\right]_{y}$ 



= Mn Iny - My I may nu

- Mn Lyy + My Ing

MyInn - Mr. Iny tand Mr Iyy - My Ing

Shear flow in Open Section:  
Shear flow is defined as the Shear force  
resistance per unit largth. Stic denoted by 9:  

$$g = \frac{Shear}{largth}$$
 w/t.  
Consider a larticlever beam of any cloading system  
in to it.  
 $dA = t ds$   
Shear Force =  $T \times dA$   
 $F = T \times t ds$   
Shear flow  $g_1 = \frac{F}{dx} = \frac{T \cdot t}{dx}$   
 $g = T \cdot t$   
Stolic quibrium  $g_1$ .  $\Sigma F = 0$   
 $u = O(AA + Ohnt (\frac{20}{35})) ds \cdot dA + T \cdot dA = 0$ 

$$\left(\frac{\partial \sigma}{\partial s}\right)$$
 ds  $\cdot$  dA = -  $T \times t \cdot ds$ 

$$\int \frac{\partial \sigma}{\partial s} ds \cdot dA = -\overline{z} \cdot t \cdot ds \cdot \int \frac{\partial \sigma}{\partial s} dA = -\overline{z} \cdot t \cdot ds \cdot \int \frac{\partial \sigma}{\partial s} dA = -\overline{z} \cdot t \\ g = \overline{z} \cdot t \\ u = -\overline{q} = \int \frac{\partial \sigma}{\partial s} dA \\ \overline{\sigma} = \begin{bmatrix} \overline{M_{y}} \underline{r}_{nn} & -M_{x} \underline{r}_{ny} \\ \overline{r}_{nx} \underline{r}_{yy} & -\underline{r}_{ny}^{2} \end{bmatrix} \mathbf{n} + \begin{bmatrix} M_{n} \underline{r}_{yy} & -M_{y} \underline{r}_{ny} \\ \overline{r}_{nx} \underline{r}_{yy} & -\underline{r}_{ny}^{2} \end{bmatrix} \mathbf{n} + \begin{bmatrix} M_{n} \underline{r}_{yy} & -M_{y} \underline{r}_{ny} \\ \overline{r}_{nx} \underline{r}_{yy} & -\underline{r}_{ny}^{2} \end{bmatrix} \mathbf{n} \\ M_{x} \Rightarrow + C \quad , M_{y} \Rightarrow -S \\ \frac{\partial M_{y}}{\partial s} = S_{x} \\ S_{x} \text{ and } S_{y} \text{ are the shear locals ading at sheas coals ading at sheas coals alog  $\frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \\ \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial s} - \frac{\partial M_{y}}{\partial s} \end{bmatrix} \mathbf{n} dA + \begin{bmatrix} \frac{\partial M_{y}}{\partial$$$

$$\frac{3}{2} - 9 = \frac{S_{x} I_{xx} - S_{y} I_{xy}}{I_{xx} I_{y} - I_{y}^{2}} \int x \cdot t ds + \frac{S_{y} I_{yy} - S_{x} I_{xy}}{I_{xx} I_{yy} - I_{y}^{2}} \int y \cdot t \cdot ds.$$

$$\frac{9}{2} = \frac{S_{y} I_{xy}}{I_{xy}} - \frac{S_{x} I_{xy}}{I_{xy}} \int n \cdot t ds + \frac{S_{x} I_{xy} - S_{y} I_{yy}}{I_{xx} I_{yy} - I_{y}^{2}} \int y \cdot t \cdot ds.$$

 $f_{1}$  the orgin of the Shear ylow is at standing of the open Section, then g = 0.

for Symmetric Sections, Ing = 0

$$\frac{1}{2} = \left[ \frac{-S_{x} \hat{I}_{xx}}{2} \int n \cdot t \cdot ds \right] + \left[ \frac{-S_{y} \hat{I}_{yy}}{2} \int y \cdot ds \right]$$

22 Problem Find the principal moment of inertia and directions of principal axis for the angle Section 1 . Shown in figure 12 cm -) 2 cm 20 5 - Josem Kennel VOY h for y 1610 Section THY X) AKED X cm<sup>2</sup>  $(\overline{E} -$ 19 T 24 6 9 -2 . **.** (\* - 4 36 2  $= \left(\frac{\Im_{nn} + \Im_{yy}}{\partial}\right) + \sqrt{\left(\frac{\Im_{y} - \Im_{nx}}{\partial}\right)^2 + \Im_{ny}^2}$ Fun  $\left(\frac{I_{yy}-I_{xx}}{2}\right)^{2} + P_{ny}$ = (Inx + Isy) -Jun a, x, + a, n2 x a,+ a2  $a_1y_1 + a_2y_2$ y 1 a, + a, = 34×6 + 36×1 24+36

= 3 cm

2 ' Parallel and theorem. X JJZXX ct

The moment of inertia of an area about an any through 0 is regual to the moment of inertia of the area labout a possible anis through the centroid C + the area multiplet by the square of distance between the ans  $\frac{1}{1}x_{\chi} = 1_{nn} + A\overline{y}^2$ 

 $\frac{T}{2}yy = \frac{T}{2}yy^{2} + A\pi^{2}$ 

Problems 1. Find the bending stress values of the points A, B, C & D for the section shown in fig. Mn = 10 KNm & My = 10 KNm Jiscm Sur Ū 200 2 3 CK 15 cm  $\mathcal{O}_{b} = \left[ \frac{M_{y} \, \widehat{I}_{nn} - M_{n} \, \widehat{I}_{ny}}{\widehat{I}_{nn} \, \widehat{I}_{yy} - \widehat{I}_{yy}^{2}} \right]_{n} + \left[ \frac{M_{n} \, \widehat{I}_{yy} - M_{y} \, \widehat{I}_{ny}}{\widehat{I}_{nn} \, \widehat{I}_{yy} - \widehat{I}_{yy}^{2}} \right]_{y}$ 0

Section	Area cm <sup>2</sup>	×	y	N 907_NN Y-7	n you Lyy n-x
	75	7.5	27.5	12.5	-5
ð	100	12.5	15	0	0
·3	75	17.5	2.5	-12.5	5
				the second second	

 $\overline{X} = \frac{a_{1}n_{1} + a_{2}n_{2} + a_{3}n_{3}}{a_{1} + a_{2} + a_{3}}$ 



144 = 5×153 = 1406.25 cm4

a parta de

$$G_{b} = \begin{bmatrix} M_{y} I_{xx} - M_{x} I_{yy} \\ f_{xx} I_{yy} - f_{y}^{2} \end{bmatrix} + \left( \frac{M_{x} I_{yy} - M_{y} I_{yy}}{f_{xx} I_{yy} - f_{y}^{2}} \right) \\ M_{x} = 10 \text{ kNm} \\ = 10 \text{ kN} \cos^{2} \text{ kN cm} \\ M_{y} = 10 \text{ kNm} \\ = 10 \text{ k} 10^{2} \text{ kN cm} \\ M_{y} = 10 \text{ kNm} \\ = 10 \text{ k} 10^{2} \text{ kN cm} \\ \end{bmatrix} \\ + \begin{bmatrix} 10 \times 10^{2} \times 47083 \cdot 33 - 10 \times 10^{2} \times (-9375) \\ J7083 \cdot 33 \times 6770 \cdot 833 - 87375^{2} \end{bmatrix} \times \\ + \begin{bmatrix} 10 \times 10^{2} \times 6770 \cdot 833 - 10 \times 10^{2} \times (-9375) \\ J7083 \cdot 33 \times 6770 \cdot 833 - 9375^{2} \end{bmatrix} \\ + \begin{bmatrix} \frac{364}{18 \times 36779/4 \cdot 9} \\ 18 \times 36779/4 \cdot 9 \end{bmatrix} + \begin{bmatrix} 16145835 \\ 1833679147 \\ 1833679147 \\ \end{bmatrix} \\ G = 0.1988 \times + 0.0880 \\ G = 0.3818 \text{ m} + 0.169 \text{ y} \quad \text{kN/cm}^{2} \\ G = 381 \cdot 8 \text{ m} + 169 \cdot 09 \text{ y} \quad \text{N/cm}^{2} \\ \end{bmatrix}$$

A is at (-12.5, 15) from Controid
$\therefore O_A = 381.8 \times -12.5 + 169.09 \times 15$
B is at (2.5, 15)
OB = 381.8x2.5 + 169.09x15
= 3490.85 N/m²
Ciat (-2.5, -15)
$G_{c} = (381.8x - 2.5) + (169.09x - 15)$
= -3490.85 N/m2
Di at (12.5, -15)
()_ = 381.8×12.5 + 169.09×(-15)
$G_{D} = 2236.15 N/m^{2}$

2. The Section Shown in fig. is Subjected to a bending moment of Mx = 30 KNM. Determine the Determine the points A B. C the corner points A, B, C & D. at bending stresses 80 cm 40 cm A 800 6 В C >x 8000 C 0 D 8cm

		1		1 100	L Jan Q I
Section	Area cm <sup>2</sup>	n Cm	cn. A	N - ST J-Y	xy-X
(1)	960	60	84	17.6	8
		3 11/1	0,08 -1-1	5	
				And and a second se	
2	640	40	40	-26.4	-12
		1.			

 $= \alpha_1 \chi_1 + \alpha_2 \chi_2 \neq$ X

 $a_1 + a_2$ 

= 960×60 + 640×40 = 5200

$\overline{Y} = \frac{a_1 y_1 + a_2 y_2}{a_1 + a_2}$
$= \frac{960 \times 84 + 640 \times 40}{1600}$ $\overline{7} = 66.4 \text{ cm}$
$\begin{aligned} \widehat{J}_{xx} &= \frac{bd^3}{12} = \frac{120 \times 8^3}{12} = 5/20 \text{ cm}^4 \\ \widehat{J}_{yy} &= \frac{8 \times 120^3}{12} = 1152000 \text{ cm}^4 \\ \widehat{J}_{xxz} &= \frac{8 \times 80^3}{12} = 341333.33 \text{ cm}^4 \\ \widehat{J}_{yyz} &= \frac{80 \times 8^3}{12} = 3413.33 \text{ cm}^4 \end{aligned}$
$\frac{G}{2xx} = (G_{xx_1} + A_1 h_1^2) + (G_{xx_2} + A_1 h_1^2)$ $= \left[ 5120 + 960 \times (17.6)^2 \right] + \left[ 341333 \cdot 3 + 640 \times (26.4) \right]$ $\frac{G}{2xx} = 302489 \cdot 6 + 787387 \cdot 73$
$\frac{f'_{XX}}{f_{YY}} = (f_{YY} + A_1 h_1^2) + (f_{YY} + A_2 h_2^2)$ $= [152000 + 960 \times 8^2] + [3+13\cdot33 + 640 \times 12^2]$

$$\frac{f_{yy}}{f_{xy}} = 1213440 + 95573.33 
= 1309013.33 cm2$$

$$\frac{f_{xy}}{f_{xy}} = A_1(n_1 - \bar{x})(y_1 - \bar{y}) + A_2(n_2 - \bar{x})(y_2 - \bar{y}) 
= 960(8)(17.6) + 640x^{-12}x^{-26.4} 
= 135168 + 202752$$

= 337920 Cm<sup>4</sup>

$$M_{\rm H} = 30 \, \text{kNm}$$
  
= 30 × 10<sup>2</sup> kN cm

$$M_{y} = 0$$

$$O = \left[ \frac{-30 \times 10^{2} \times 337920}{(1089877.33 \times 1309013.33) - 337920^{2}} \right] \chi$$

$$+ \left[ \frac{30 \times 10^{2} \times 1309013.33}{(1089877.33 \times 1309013.33) - 337920^{2}} \right] Y$$

$$\int = -7 \cdot 7 \cdot 240 \times 10^{-4} + 2 \cdot 9 \times 10^{-3} y$$

$$\int = -0.000772 \times + 0.0029 y \times 10/cm^{2}$$

$$A(-52, 21.6)$$

$$B(68, 13.6)$$

$$c(-52, 13.6)$$

$$p(-16, -66.4)$$

$$d A,$$

$$\int A = -0.000772 \times (-52) + 0.0029 \times 21.6$$

$$\int A = -0.1027 \times 10^{-5} \text{ cm}^{2}$$

$$d B,$$

$$\int B = -0.000772 (68) + 0.00297 \times 13.6$$

$$\int B = -0.01292 \times 10/cm^{2}$$

$$G = -0.000772 (-52) + 0.0029 \times 13.6$$

$$= 0.079 \times 10/cm^{2}$$

$$d B$$

 $\overline{O_{p}} = -0.000772 (-16) + 0.0029 (-66.4)$ 

= - 0.186 KN/cm² (-ve sign indicals compression.

3. An angle section Shown in fig. is Subjected to Mx = 20 KNM & My = 15 KNM. Find the manimum bending Stress . TB 17 0 1500 6 D Tim 0 UK 15 cm > 4-1206

Section	Area cm <sup>2</sup>	2 670	y Cn	h for Inx y-y co	to for Ly -R-X con
le l	14	0.5	8	3.879	
2	15	7.5	0.5	- 3.6206	3-379

 $\overline{X} = \frac{q_1 \chi_1 + q_2 \chi_2}{q_1 + q_2} = \frac{14 \times 0.5 + 15 \times 7.5}{14 + 15} = 4 \cdot 1206 \text{ cm}$ 

 $\overline{y} = \frac{q_1 y_1 + q_2 y_2}{q_1 + q_2} = \frac{14 \times 8 + 15 \times 0.5}{14 + 15}$ 

= 4.1206 cm

$$\begin{split} \widehat{G}_{nn_{1}} &= \frac{bd^{3}}{i2} = \frac{i \times i + i^{3}}{i2} = 2i \cdot 8 \cdot 66 \, \mathrm{cm}^{4} \\ \widehat{G}_{nn_{2}} &= \frac{15 \times i^{3}}{i2} = -i \cdot 25 \, \mathrm{cm}^{4} \\ \widehat{G}_{yy_{1}} &= \frac{i \times i^{3}}{i2} = -i \cdot 25 \, \mathrm{cm}^{4} \\ \widehat{G}_{yy_{2}} &= \frac{db^{2}}{i2} = -\frac{i \times 15^{2}}{i2} = -d \cdot 8i \cdot 25 \, \mathrm{cm}^{4} \\ \widehat{G}_{xx} &= (\widehat{G}_{nn_{1}} + A_{1} \cdot b_{1}^{2}) + (\widehat{G}_{nn_{2}} + A_{2} \cdot b_{2}^{2}) \\ &= (3 \cdot 28 + i + 3 \cdot 3 \cdot 879^{2}) + (i \cdot 25 + i 5 \times (-3 \cdot 6206)^{2}) \\ \widehat{G}_{xx} &= 63 \cdot 7 \cdot 7 \, \mathrm{cm}^{4} \\ \widehat{G}_{yy} &= (\widehat{G}_{yy_{1}} + A_{1} \cdot b_{1}^{2}) + (\widehat{G}_{yy_{2}} + A_{2} \cdot b_{2}^{2}) \\ &= \left[i \cdot 66 + i + (-3 \cdot 6206)^{2}\right] + \left[-28i \cdot 25 + i \cdot 5 \left(3 \cdot 379\right)^{2}\right] \\ \widehat{G}_{yy} &= 63 \cdot 7 \cdot 202 \, \mathrm{cm}^{4} \\ \widehat{G}_{xy} &= A_{i} \left(x_{i} - \overline{x}\right) \left(y_{i} - \overline{y}\right) + A_{2} \left(x_{2} - \overline{x}\right) \left(y_{2} - \overline{y}\right) \\ &= i + \left(0 \cdot 5 - 4 \cdot i \cdot 206\right) \left(8 - 4 \cdot i \cdot 206\right) + i \\ i \cdot 5 \left(-3 \cdot 6206\right) \left(3 \cdot 379\right) \\ \widehat{G}_{xy} &= -3 \cdot 80 \cdot 15 \, \mathrm{cm}^{4} \end{split}$$

$$\begin{aligned} 
\begin{aligned}
& \mathcal{O}_{A} = (6 \cdot 566 \times -4 \cdot 1206) + (7 \cdot 054 \times 10 \cdot 879) \\
&= 49 \cdot 720 \quad kns/cm^{2} \\
& \mathcal{O}_{B} = (6 \cdot 566 \times -3 \cdot 1206) + (7 \cdot 054 \times 10 \cdot 879) \\
&= 56 \cdot 28 \quad kn/m^{2} \\
& \mathcal{O}_{C} = (6 \cdot 566 \times -4 \cdot 1206) + (7 \cdot 054 \times -4 \cdot 1206) \\
&= .-56 \cdot 08 \quad kn/m^{3} \\
& \mathcal{O}_{D} = (6 \cdot 566 \times -3 \cdot 1206) + (7 \cdot 054 \times -3 \cdot 1206) \\
&= -42 \cdot 4 \quad kn/m^{2} \\
& \mathcal{O}_{E} = (6 \cdot 566 \times 10 \cdot 879) + (7 \cdot 054 \times -3 \cdot 1206) \\
&= 49 \cdot 36 \quad kn/m^{2} \\
& \mathcal{O}_{F} = (6 \cdot 566 \times 10 \cdot 88) + (7 \cdot 054 \times -4 \cdot 12) \\
&= 42 \cdot 31 \\
& \therefore \text{ Al } \text{ Pl. B tensile Stress is monimum and all point C, Compressive Stress is monimum.
\end{aligned}$$

$$\begin{aligned}
\mathbf{G} &= \left[ \frac{M_y \Gamma_{NN} - M_N \Gamma_{Ny}}{\Gamma_{NN} \Gamma_{yy} - \Gamma_{yy}} \right]_N + \left[ \frac{M_N \Gamma_{yy} - M_y \Gamma_{yy}}{\Gamma_{NN} \Gamma_{yy} - \Gamma_{yy}^2} \right]_d \\
M_n &= 20 \times 10^2 \text{ ANV CM} \\
M_y &= 15 \times 10^2 \text{ KNCm} \\
\mathbf{G} &= \left[ \frac{15 \times 10^2 \times 637 \cdot 17 - 20 \times 10^2 \times -380 \cdot 15}{(837 \cdot 17 \times 637 \cdot 202) - (-380 \cdot 15)^2} \right]_N \\
+ \left[ \frac{20 \times 10^2 \times 637 \cdot 202 - 15 \times 10^2 (-380 \cdot 15)}{(637 \cdot 17 \times 637 \cdot 202) - (-380 \cdot 15)^2} \right]_d \\
\mathbf{G} &= 6 \cdot 566 \times + 7 \cdot 05 \cdot 4 \text{ Y} \\
A &(-4 \cdot 1206, 10 \cdot 879) \\
B &(-3 \cdot 1206, 10 \cdot 879) \\
C &(-4 \cdot 1206, -4 \cdot 1206) \\
D &(-3 \cdot 1206, -3 \cdot 1206) \\
E &(10 \cdot 879, -3 \cdot 1206) \\
F &(10 \cdot 879, -4 \cdot 1206)
\end{aligned}$$

Shear flow in Open Section - Problems

1. Calculate the Shear flow and Shear Certer for the Section Shown in fig. The section is Subjected a shear force of I KN in vertical and horizontal directions, bumped aleas at A, B, C & D are 4m², am<sup>2</sup>, am<sup>2</sup> a 6m<sup>2</sup> respectively. 30m 100 30 m > X Iom

Member	Area m <sup>2</sup>	X	y	h for Inn 4-7	h yor Iyy x-x
ĥ	4	0	0	-17.142	-2.857
В	2	10	0	-17-142	7 • 143
c	2	10	30	12.828	7./43
٦	6	0	30	12.858	-2 .857

 $\overline{X} = \frac{a_1n_1 + a_2n_2 + a_3n_3 + a_4n_4}{a_4n_4}$  $a_1 + a_2 + a_3 + a_4$  $= (4 \times 0) + (2 \times 10) + (2 \times 10) + (6 \times 0)$ 4+2+2+6

$$\begin{split} \overline{\chi} &= \pounds \cdot 857 \text{ m} \\ \overline{\chi} &= \frac{a_1 g_1 + a_2 g_2 + a_3 g_3 + a_4 g_4}{a_1 + a_2 + a_3 + a_4} \\ &= \frac{(4 \times 0) + (4 \times 0) + (4 \times 30) + (6 \times 30)}{4 + 4 + 4 + 4} \\ \overline{\chi} &= 17.14 \text{ m} \\ \overline{\chi} &= 17.14 \text{ m} \\ \overline{\chi} &= 4 \times (-17.14 \text{ a})^2 + 4 \left(-17.14 \text{ a}\right)^2 + 4 \left(14.858\right)^2 + 6 \left(44.858\right)^2 \\ &= 30.85 \cdot 90.6 \text{ m}^4 \\ \overline{\chi} &= 4 \left(-4 \cdot 857\right)^2 + 4 \left(7.143\right)^2 + 4 \left(7.143\right)^4 + 6 \left(-2.857\right)^2 \\ &= 385 \cdot 7 \text{ m}^4 \\ \overline{\chi} &= 4 \left(-4.857\right) \left(-17.142\right) + 4 \left(7.143\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) + 4 \left(7.143\right) \left(-17.142\right) + 4 \left(7.143\right) + 4 \left(7$$

$$\begin{aligned} G_{022}(i) \\ S_{x} &= 0, \quad S_{y} = 1 \text{ kN} = 1000 \text{ N} \\ g &= \left[ \frac{1000 \times (-85 \cdot 7i) - 0}{3085 \cdot 906 \times 285 \cdot 7 - (85 \cdot 7)^{2}} \right] \text{ A}_{i} \text{ X}_{i} \quad + \\ & \left[ \frac{0 - (1000 \times 285 \cdot 7)}{(3085 \cdot 706 \times 285 \cdot 7)(85 \cdot 7)^{2}} \right] \text{ A}_{i} \text{ Y}_{i} \\ g &= -0 \cdot 098 \text{ A}_{i} \text{ X}_{i} \quad -0 \cdot 326 \text{ A}_{i} \text{ Y}_{i} \\ g &= (-0 \cdot 098 \text{ A}_{i} \text{ X}_{i} \quad -0 \cdot 326 \text{ A}_{i} \text{ Y}_{i} \\ g &= 23 \cdot 473 \text{ N/m} \\ g &= 33 \cdot 29 \text{ N/m} \\ g_{cb} &= 9 \text{ A}_{bc} + \left[ -0 \cdot 098 \times 2 \times 7143 - (0 \cdot 326 \times 2 \times 77142) \right] \\ &= 33 \cdot 29 \text{ N/m} \\ g_{cb} &= 9 \text{ A}_{bc} + \left[ -0 \cdot 098 \times 2 \times 7143 - (0 \cdot 326 \times 2 \times 12 \cdot 858) \right] \\ &= 23 \cdot 506 \text{ N/m} \end{aligned}$$

$$D = \frac{23 \cdot 50^{10} \text{ M/m}}{10}$$

$$D = \frac{23 \cdot 50^{10} \text{ M/m}}{10}$$

$$30 \text{ T} = \frac{33 \cdot 29 \text{ M/m}}{10}$$

$$Shear flow = \frac{Sher forme}{10^{10} \text{ Kength}}$$

$$R = \frac{10}{23 \cdot 473} \frac{10}{10}$$

take moment about D,

 $S_y \times C_x = (23 \cdot 473 \times 10 \times 30) + (33 \cdot 29 \times 30 \times 10)$ 

1000 x en = 17028.9

$$P_{n} = 17.03 m$$

Case (ii)

$$S_n = 1000 N, S_y = 0$$

$$\begin{aligned}
\mathcal{P} &= \left[ \frac{0 - 1000 \times 3085}{3085 \times 285 \cdot 7 - (85 \cdot 7)^2} \right] A; \chi; + \left[ \frac{1000 \times (-85 \cdot 7) - 0}{3085 \times 285 \cdot 7 - (85 \cdot 7)^2} \right] A; \chi;
\end{aligned}$$

9 = -3.529 A; X; = -0.098 A; y;

 $\begin{aligned} & 2_{AB} = (-3.529 \times 4 \times -2.857) - (0.098 \times 4 \times (-17.14^2)) \\ & = 47.049 \, \text{N/m} \end{aligned}$ 

$$g_{bc} = g_{nb} + \left[ -3 \cdot 527 \times d \times 7/43 - 0 \cdot 098 \times 2 \times (-17 \cdot /43) \right]$$

$$= -0 \cdot 0064$$

$$g_{bc} \approx 0$$

$$g_{bc} = g_{bc} + \left[ -3 \cdot 527 \times d \times 7 \cdot 143 - 0 \cdot 098 \times 2 \times 12 \cdot 855 \right]$$

$$= -52 \cdot 93$$

$$y \xrightarrow{-52 \cdot 93}$$

Thin Walled Section - Problems:

- 1. Determine the show flow distribution in the thin walled Z-section shown in yig, which is subjected to a Shear load Sy applied through the shear Centre of the Section.

  - $S_{y} \supseteq given$   $:S_{n} = 0$   $9 = \frac{S_{y} \Sigma_{ny} - S_{n} \Sigma_{nn}}{S_{nn} \Sigma_{yy} - S_{y}^{2}} \int n t ds + \frac{S_{n} \Sigma_{ny} - S_{y} \Sigma_{yy}}{S_{nn} \Sigma_{yy} - S_{y}^{2}} \int y \cdot t ds.$  $S_{m} = 0$
  - $\frac{1}{2} = \frac{S_y \Gamma_{ny}}{\Gamma_{nx} \Gamma_{yy} \Gamma_{ny}^2} \int n t ds = \frac{S_y \Gamma_{yy}}{\Gamma_{nx} \Gamma_{yy} \Gamma_{ny}} \int y t ds$

2 = Sy Inn Lyy - Ly fly neds - Tyy Jyeds.

x

$$\int \frac{1}{2} \int \frac{$$

$$\int \int = 2 \left[ \frac{y_{1}xt \times \frac{y_{4} \times \frac{y_{2}}{2}}{\frac{1}{268}} + \frac{1}{268} + \frac{1}{268} \right]$$

$$= \frac{2}{10} \left[ \frac{\frac{th^{3}}{168}}{\frac{1}{268}} \right]$$

$$= \frac{5y}{\left(\frac{\frac{th^{3}}{3} \times \frac{th^{3}}{24}\right) - \left(\frac{\frac{th^{3}}{2}}{\frac{1}{28}}\right)^{2}}{\frac{\frac{th^{3}}{8}}{\frac{1}{8}} + \frac{1}{268}} \right] \left[ \frac{\frac{th^{3}}{8}}{\frac{1}{8}} + \frac{1}{268} + \frac{\frac{th^{3}}{12}}{\frac{1}{2}} \right] y t du$$

$$= \frac{5y}{\frac{\frac{th^{6}}{36}}{\frac{\frac{th^{2}}{36}}{\frac{1}{2}}} \left[ \frac{\frac{th^{3}}{8}}{\frac{1}{8}} + \frac{1}{268} + \frac{\frac{th^{3}}{12}}{\frac{1}{2}} \right] y t du$$

$$= \frac{5y}{\frac{64t^{2}h^{6}}{36}} - \frac{t^{2}h^{6}}{\frac{64}{64}} \left[ \frac{\frac{th^{3}}{8}}{\frac{1}{8}} + \frac{1}{22} \right] y t du$$

$$= \frac{5y \times 2304}{\frac{28}{6}t^{2}h^{6}h^{3}}{\frac{1}{2}} \left[ \frac{\frac{th^{3}}{8}}{\frac{1}{8}} + \frac{1}{2} \right] y t du$$

$$= \frac{10 \cdot \frac{28}{8}}{h^{3}} \int x du$$

$$= \frac{10 \cdot \frac{28}{8}}{h^{3}} \int x du$$

В
Consider bottom florage, 
$$\frac{1}{2}$$
  
 $\chi = -\frac{1}{2}\frac{1}{2}\frac{1}{5}$ ,  $\chi = -\frac{1}{2}\frac{1}{2}\frac{1}{5}\frac{1$ 

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$$\begin{aligned} g_{3} &= \frac{S_{3}}{h^{3}} \left[ -i \cdot 7_{2} \times \frac{h^{3}}{2} + \frac{5 \cdot i_{4} \cdot h^{2}}{4} \right] + 0 \\ &= -\frac{0 \cdot 86 \cdot S_{3}}{h} + \frac{i \cdot 285 \cdot S_{3}}{h} \\ \hline g_{13} &= \frac{0 \cdot 425 \cdot S_{3}}{h} \\ \hline g_{13} &= \frac{0 \cdot 425 \cdot S_{3}}{h} \\ \hline g_{23} &= -\frac{6 \cdot 85}{h^{3}} \cdot S_{3} \int_{0}^{5} \left( -\frac{L}{2} + S_{2} \right) dS_{3} + g_{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L}{2} + \frac{S_{3}}{2} \right) dS_{3} + g_{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{2}}{2} + \frac{S_{3}^{2}}{2} \right)^{5} + g_{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{2}}{2} + \frac{S_{3}^{2}}{2} \right)^{5} + g_{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{2}}{2} + \frac{S_{3}^{2}}{2} \right)^{5} + g_{3} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{2}}{2} + \frac{S_{3}^{2}}{2} \right)^{5} + g_{3} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} + \frac{3 \cdot 425 \cdot S_{3}^{2} \times S_{3}}{h^{3}} + g_{3} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{2} - \frac{6 \cdot 85 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot S_{3}}{h^{3}} \int_{0}^{5} \left( -\frac{L \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3}} + \frac{2}{2} \\ &= -\frac{6 \cdot 85 \cdot 5 \cdot S_{3}}{h^{3}} - \frac{1 \cdot 4 \cdot 5 \cdot S_{3}}{h^{3$$

h

d Pt·3  

$$S_{y} = h$$

$$P_{3} = \frac{3 \cdot 4 \cdot 35 \times S_{y} \times h^{y}}{h^{1}} - \frac{3 \cdot 4 \cdot 25 \times S_{y} \times h^{y}}{h^{3}} + P_{z}$$

$$= \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h} - \frac{3 \cdot 25 \cdot 32 \cdot 4 \cdot 25 \cdot S_{y}}{h} + \frac{9}{h^{3}}$$

$$P_{z} = \frac{9 \cdot 4 \cdot 25 \cdot S_{y}}{h}$$

$$P_{z} = \frac{9 \cdot 4 \cdot 25 \cdot S_{y}}{h}$$

$$P_{z} = \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} - \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} + \frac{9}{h^{2}}$$

$$P_{z} = \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} - \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} + \frac{9}{h^{2}}$$

$$= \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} - \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} + \frac{9}{h^{2}}$$

$$= \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} - \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} + \frac{9}{h^{2}}$$

$$= \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} - \frac{3 \cdot 4 \cdot 25 \cdot S_{y}}{h^{2}} + \frac{9}{h^{2}}$$

$$= \frac{1 \cdot 7 \cdot 125 \cdot S_{y}}{h} + \frac{9 \cdot 4 \cdot 25 \cdot S_{y}}{h}$$

$$P_{xid} = \frac{S_{y}}{h} \times 1 \cdot 281$$

$$P_{xid} = \frac{1 \cdot 381 \cdot S_{y}}{h}$$

$$\int_{A} \int_{A} \int_{A$$

-

" Calculate the position of shear centre of the thin walled Channel Section shown in Vig. The Thickness 't' 0 the wall is Constant 13 This Cross Section is Symmetry about n- aris s. Shear Centre lies on the X aris . I'my = 0 Ps = - (Sn Inn - Sy Ing) Inn Igy - Ing (t nots - Sy Jy - Sn Ing) Inn Egy - Ing (ty ds Sn = 0, Iny = 0  $\frac{1}{2} = -\frac{Sy \, \underline{I} \, \underline{yy}}{\underline{I} \, \underline{xy}} \left[ \underline{ty} \, d\underline{s} \right]$ = - Jy tydo  $\frac{f_{xx}}{l_{2}} = 2 \left[ \frac{bt^{3}}{l_{2}} + bt \times \left( \frac{h}{2} \right)^{2} \right] + \frac{t \times h^{3}}{l_{2}}$  $= 2 \left[ \frac{bt^3}{12} + \frac{bth^2}{4} \right] + \frac{th^3}{12}$ Notecting higher pidas of t 1 Jak  $\frac{4}{2}nn = \frac{bth^2}{2} + \frac{th^3}{12}$ 

$$\frac{G}{f_{NR}} = \frac{th^{3}}{iz} \left[ 1 + \frac{6h}{h} \right]$$

$$\frac{g}{s} = \frac{-S_{y}}{\frac{th^{3}}{iz} \left(1 + \frac{6h}{h}\right)} \int_{s}^{s} t y ds$$

$$= \frac{-S_{y} \times 12}{\frac{th^{3'}(h + \frac{6h}{h})}{h^{2'}(h + \frac{6h}{h})}} \int_{s}^{s} y ds$$

$$= \frac{-S_{y} \times 12}{h^{2'}(h + \frac{6h}{h})} \int_{s}^{s} y ds$$

$$= \frac{-S_{y} \times 12}{h^{2}(6b + h)} \int_{0}^{s} y ds$$

$$= \frac{-S_{y} \times 12}{h^{2}(6b + h)} \int_{0}^{s} -\frac{1}{2} ds$$

$$= \frac{-12S_{y}}{h^{2}(6b + h)^{2}} \int_{0}^{s} hS_{z} \int_{0}^{s} \int_{0}^{s} ds$$

$$= \frac{-6S_{y}}{h^{2}(6b + h)} \int_{0}^{s} hS_{z} \int_{0}^{s} \int_{0}^{s} ds$$

$$= \frac{-6S_{y}}{h^{2}(6b + h)} \int_{0}^{s} hS_{z} \int_{0}^{s} \int_{0}^{s} ds$$

$$\frac{G}{h^{2}(6b + h)} \int_{0}^{s} hS_{z} \int_{0}^{s} \int_{0}^{s} ds$$

$$= \frac{6S_{y}}{h^{2}(6b + h)} \int_{0}^{s} hS_{z} \int_{0}^{s} \int_{0}^{s} ds$$

$$\frac{G}{h^{2}(6b + h)} \int_{0}^{s} \int$$

In web, 
$$y = -\frac{1}{2} + \frac{5}{2}$$
  

$$g_{23} = \frac{-S_{1} \times 12}{h^{2}(6b+h)} \int (-\frac{1}{2} + \frac{5}{2} + \frac{5}{2}) dx_{1} + \frac{9}{2} + \frac{5}{2} + \frac{9}{2} + \frac{12}{2} + \frac{12}{2}$$

$$f_{h} \quad \text{usb}, \quad y = -\frac{h}{2} + S_{a}$$

$$g_{a3} = \frac{-S_{a} \times 12}{h^{2}(6b+h)} \int_{0}^{s} (-\frac{h}{2} + S_{a}) ds_{a} + \frac{g_{a}}{2}$$

$$= -\frac{S_{a} \times 12}{h^{2}(6b+h)} \int_{0}^{s} (-\frac{h}{2} + \frac{S_{a}}{2}) \int_{0}^{s} + \frac{g_{a}}{2}$$

$$g_{a3} = -\frac{6S_{a}}{h^{2}(6b+h)} \int_{0}^{s} \left[S_{ab}^{2} - hS_{a}\right]_{0}^{32} + \frac{g_{a}}{2}$$

$$g_{a3} = h$$

$$= \frac{-6S_{a}}{h^{2}(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h^{2}(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h^{2}(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h^{2}(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h^{2}(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

$$g_{a3} = \frac{-6S_{a}}{h(6b+h)} \int_{1}^{b} \left[h^{2} - h^{2}\right] + \frac{g_{a}}{2}$$

take mont wir to x aims  $S_y \times e_n = 2 \int_0^b \frac{9}{12} \frac{ds_i(h/2)}{ds_i(h/2)}$  $= 2 \int \frac{16}{16} \frac{6}{5} \frac{5}{5} \frac{5}{5} \frac{1}{5} \frac{x}{6} \frac{ds}{ds} \frac{x}{ds} \frac{k}{2}$  $= \frac{6 s_y}{(6b+h)} \begin{bmatrix} s_i \\ z \end{bmatrix}_0^b$ Siden =  $\frac{3 s_y}{(6b+h)}$  $C_n = \frac{36^2}{6.64h}$  (4.10)  $\int_{3} = \frac{6}{5} \frac{5}{5} \frac{5}{5} \frac{5}{5}$ 2 1 Commence ? A jea diga A. (dhaisyid

Shear flow in Closed Section due to Torsion (using Breat Batto formula) (JTorque (T) - To Ja T adda to Rodin (V) おそしまれた If the loads are applied away from the Shear Center, torsion besides bending also occurs. Therefore the beam is Subjected to Stress due to torsion and bending. lorsion Causes a twisting Stress 'I' also called Shean stress and a rotation called Shear Strain ?. Torsional moment increases linearly as shear strain in it increases on the clemental area of length do' and 'r' aubor Ex 8 x3 1. 9= Txt

For sional momend.  

$$dT = dF'r$$

$$dT = Ix ds \cdot txr$$

$$\int dT = \int I \times ds \cdot txr$$

$$\int dT = \int I \times ds \cdot tr$$

$$= \int r \cdot ds \cdot Txt$$

$$\int dT = \int \int g \cdot ds \cdot r$$

$$T = g \int dA \cdot r$$

$$T = g \int 2dA$$

$$T = \frac{g}{2} dA$$

$$du = \frac{g}{2} \times Tx \nabla \times Volume$$

$$du = \frac{g}{2} \times Tx (\frac{T}{6}) \times dA \times t \times da$$

$$du = \frac{g}{2} \times \frac{T^{2}}{6} \times dA \times t \times da$$

$$du = \frac{g^{2}}{26} \int dA \times da$$

1. Find the Shear flow per unit length of a two Cell tube both made of AI, and G = 2.69 × 10'° Pa Subjected to a torque of 90000 Nem.



Griven

 $G = 2.69 \times 10^{10} R$  T = 90000 N cm= 900 Nm

$$T = 2A_{1}Q_{1} + 2A_{2}Q_{2}$$

$$900 = 2 \times \left[0.2 \times 0.35\right]Q_{1} + 2 \left[\frac{\pi \times (0.1)^{2}}{2}\right]Q_{2}$$

$$0.14Q_{1} + 0.0314Q_{2} = 900 \quad --0$$

Angle of twist is  

$$\theta = \frac{1}{2AG} - \frac{9}{E} \int ds$$
  
 $\theta_{1} = \frac{1}{2XO(2 \times 0.35 \times 2.69 \times 10^{10})} \int \frac{9}{0.002} \times 0.2 + \frac{9}{0.001} \times 0.35$ 

$$\frac{+\frac{\gamma_{1}}{0.001}}{\theta_{1}} \times 0.35 + \frac{\gamma_{1} - \gamma_{2}}{0.0015}} \times 0.2$$

$$\theta_{1} = 2.655 \times 10^{-10} \left[ \frac{1009}{9} + 7009 + 133.33 (9.-9_{2}) \right]$$

$$\begin{array}{l} \theta_{1} = \frac{2}{2} \cdot 655 \times 10^{-10} \left[ 800 \, 9_{1} + 133 \cdot 33 \, 9_{1} - 133 \cdot 33 \, 9_{2} \right] \\ \theta_{1} = \frac{2}{2} \cdot 477 \times 10^{-7} \, 9_{1} - 3 \cdot 539 \times 10^{-7} \, 9_{2} \\ \theta_{1} = \frac{2}{2} \cdot 477 \times 10^{-7} \, 9_{1} - 0 \cdot 3539 \times 10^{-7} \, 9_{2} \\ \theta_{2} = \frac{1}{2 \times \frac{\pi \times (0^{-1})^{2}}{2}} \frac{2}{2} \cdot 69 \times 10^{10}} \left[ \frac{9_{2} - 9_{1}}{0 \cdot 0015} \times 0 \cdot 2 + \frac{9_{2}}{0 \cdot 001} \right] \\ \theta_{2} = 1 \cdot 183 \times 10^{-7} \left[ (9_{2} - 9_{1}) \times 133 \cdot 33 + 9 \cdot 314 \cdot 157 \, 9_{2} \right] \\ \theta_{3} = 1 \cdot 183 \times 10^{-7} \left[ 4 + 7 \cdot 489 \, 9_{2} - 133 \cdot 33 \, 9_{1} \right] \\ \theta_{4} = 1 \cdot 183 \times 10^{-7} \left[ 4 + 7 \cdot 489 \, 9_{2} - 133 \cdot 33 \, 9_{1} \right] \\ \theta_{4} = -1 \cdot 577 \, 10^{-7} \, 9_{1} + 5 \cdot 273 \times 10^{-7} \, 9_{2} \right] \\ \theta_{4} = -1 \cdot 577 \, 7 \times 10^{-7} \, 9_{1} + 5 \cdot 273 \times 10^{-7} \, 9_{2} \\ \psi_{2} = \left( \frac{2}{4} \cdot 477 \, 9_{1} - 0 \cdot 3539 \, 9_{2} \right) \times 10^{-7} = \left( -1 \cdot 577 \, 9_{1} + 5 \cdot 273 \, 9_{1} \right) \\ \psi_{4} = 4779 \, 9_{1} - 0 \cdot 3539 \, 9_{2} \right) \times 10^{-7} = \left( -1 \cdot 577 \, 9_{1} + 5 \cdot 273 \, 9_{1} \right) \\ \psi_{4} = 4779 \, 9_{1} - 0 \cdot 3539 \, 9_{2} \right) \times 10^{-7} = \left( -1 \cdot 577 \, 9_{1} + 5 \cdot 273 \, 9_{1} \right) \\ \psi_{4} = 4779 \, 9_{1} - 0 \cdot 3539 \, 9_{2} \right) = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{2} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{1} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{2} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{2} - 5 \cdot 646 \, 9_{2} = 0 \\ \psi_{1} = 0.49 \, 9_{2} - 0 \\ \psi_{1} = 0.49 \, 9_{1} - 0 \cdot 0 \\ \psi_{1} = 0.49 \, 9_{2} - 0 \\ \psi_{1} = 0.49 \, 0 \\ \psi$$

$$-17000 = \left[ 2 \times \overline{\pi} \frac{(0\cdot2)^2}{2} \times \gamma_1 \right] + \left[ 3 \times 0.4 \times 0.4 \right] \gamma_2 + \left[ 2 \times 0.4 \times 0.4 \right] \gamma_3$$

$$= \frac{1}{2 \times 0.4 \times 0.4} \gamma_4$$

$$= \frac{1}{2 \times 0.4 \times 0.4} \left[ 2 \times 0.4 \times 0.4 \times 0.4 \times 0.4 + \frac{1}{2} \gamma_4 + 80 \gamma_4 + \frac{1}{2} \gamma_4 + \frac{1}{2}$$

the state of the press in the

$$\begin{aligned} \partial_{2} &= \frac{3 \cdot 125}{G} \left[ -80q_{1} + 479 \cdot 79 \cdot q_{2} - 133 \cdot 33 \cdot q_{3} \right] \quad (3) \\ \eta^{\text{vr}} \quad \text{Cell } 3, \\ \partial_{3} &= \frac{1}{2 \times 0 \cdot (1 \times 0 \cdot 1 \times G_{1})} \left[ \frac{q_{3} - q_{2}}{0 \cdot 003} \times 0 \cdot 4 + \frac{q_{3}}{0 \cdot 003} \times 0 \cdot 4 + \frac{q_{3}}{0 \cdot 003} \times 0 \cdot 4 \right] \\ \partial_{3} &= \frac{3 \cdot 125}{G} \left[ 133 \cdot 33 \left( q_{3} - q_{2} \right) + 366 \cdot 66 \cdot q_{3} + 100 \cdot q_{3} \right] \\ \partial_{3} &= \frac{3 \cdot 125}{G} \left[ -133 \cdot 33 \left( q_{3} - q_{2} \right) + 366 \cdot 66 \cdot q_{3} + 100 \cdot q_{3} \right] \\ \partial_{3} &= \frac{3 \cdot 125}{G} \left[ -133 \cdot 32 \cdot q_{2} + 4 \cdot 99 \cdot 99 \cdot 99 \cdot q_{3} \right] \\ \partial_{3} &= \frac{3 \cdot 125}{G} \left[ -133 \cdot 32 \cdot q_{2} + 4 \cdot 99 \cdot 99 \cdot q_{3} \right] \\ \partial_{4} &= 0 + 100 \cdot q_{4} + 100 \cdot q_{5} + 10$$

also,  $O_2 = O_3$ 

 $:\frac{3\cdot 125}{6} \left[ -\frac{809}{7} + 479\cdot 999}{2} - \frac{133\cdot 339}{3} \right] = \frac{3\cdot 125}{6} \left[ -\frac{133\cdot 339}{7} + 499\cdot 999}{3} \right]$ 

 $-809, + 479.99.9, + 133.339_3 - 133.339_3 - 499.999_3 = 0$  $\omega - 809 + 613 \cdot 329 - 633 \cdot 329 = 0$ C By solving (), () & () we get 2, , 2, 23  $0.12569, +0.329, +0.329_3 = -19000$  $\odot$  $923.5589, -683.679 + 133.339_3 = 0$  $\textcircled{\basis}$  $-809, + 613.329_{2} - 633.329_{3} = 0$ 6 9:= -17039.059 N/m 92 = -27859-656 N/m  $q_3 = -24827 - 512$  N/m 7.151 - 301 - 327 4 - 803 1923 1987 - 642 di J. + 183 42

3. Find the Shear flow per wit length of a two cell tube both made of Al and G = 2.69 × 10' Pa, Subjected to a torque of 60 kNm To find x use Pythogores theorem × 40cm (3)  $\chi^2 = 50^2 + 20^2$  $\chi^2 = \sqrt{2900}$ n = 53.85 cm к 60 cm \* Soon + = 0.5385 m Given, grap J. T= 60 KNM S x ( z ox b ox ) x S. = 60000 NM Since the wall thickness is not given, let us unit Hickness - t assume it to be G = 2.69 × 10° Pa (001) NS 0 T= 2A,9, + 2A,9,  $60000 = (2 \times 0.4 \times 0.6)q_{1} + (2 \times \frac{1}{2} \times 0.4 \times 0.5)q_{2}$  $\omega 0.489, + 0.0209_2 = 60000 - 0$ we know angle of twist,  $O = \frac{1}{2AG} + \frac{2}{t} \int ds$ 

5. 41669, -833.29 = -20009, +73859 = 061669, - 8218.29, = 0 G By solving OR @ we get 2, \* 9/2 0.489, + 0.209 = 6000061669, - 8218.29 = 0 G 9, = 95229.45 N/m 92= 71,449.31N/m

## Unit III Structural Idealization.

1. (212 12) 245

1. Part of a wing section is in the form of the two call box shown in which the vortical spars are connected to one wing skin through angle sections all having a 'Cross' Sectional areat of 300 min<sup>2</sup>. Idealize the Section into an arrangement of direct stress Carrying booms and shown Stress only Grrying parels Switable for resisting bending moments in a vertical plane. Resistion

the booms at the span/Skin junctions.



$$B_{1} = \frac{tb}{6} \left( 2 + \frac{\sigma_{2}}{\sigma_{1}} \right) + \frac{tb}{6} \left( 2 + \frac{\sigma_{2}}{\sigma_{1}} \right) + \frac{300}{6} \right)$$
$$= \frac{3 \times 400}{6} \left( 2 + \frac{-200}{+200} \right) + \frac{3 \times 600}{6} \left( 2 + \frac{150}{200} \right) + 300$$

 $B_{6} = B_{1} = 1050 \, \text{mm}^{2}$ 

Dr. Ajik Ry R

Plens Mecer

$$B_{2} = 300 + 300 + \frac{4b}{6} - \left(2 + \frac{5}{5(2)}\right) + \frac{4b}{6} \left(2 + \frac{5}{3(2)}\right) + \frac{4b}{6} \left(2 + \frac{5}{3(2)}\right) + \frac{4b}{6} \left(3 + \frac{5}{5(2)}\right)$$

$$B_{2} = B_{3} = 300 + \frac{4b}{6} - \left(2 + \frac{5}{3(2)}\right) + \frac{4b}{6} - \left(2 + \frac{5}{5(2)}\right)$$

$$= 871 \text{ mm}^{2}$$

$$A_{3} = B_{3} = 300 + \frac{4b}{6} - \left(2 + \frac{5}{3(2)}\right) + \frac{4b}{6} - \left(2 + \frac{5}{5(2)}\right)$$

$$A_{3} = \frac{1}{3(2)} + \frac{1}{3(2)} +$$

0,

$$B_{i} = 1000 + \frac{tb}{6} \left(2 + \frac{\sigma_{2}}{\sigma_{1}}\right) + \frac{tb}{6} \left(2 + \frac{\sigma_{4}}{\sigma_{1}}\right)$$

$$= 1000 + 10 \times 500 - \left(2 + \frac{150}{150}\right) + 10 \times \frac{300}{6} \left(2 + \frac{-150}{150}\right)$$

$$= 1000 + 10 \times 500 - \left(2 + 1\right) + 10 \times 300 - \left(2 - 1\right)$$

$$B_{i} = B_{i} = 4000 \text{ mm}^{2}$$

$$8_{3} = \frac{656}{600} + \frac{16}{6} \left( 2 + \frac{0}{02} \right) + \frac{16}{6} \left( 2 + \frac{0}{02} \right)$$
  
=  $\frac{656}{600} + \frac{10 \times 500}{6} \left( 2 + \frac{150}{150} \right) + \frac{8 \times 300}{6} \left( 2 + \frac{-150}{150} \right)$   
=  $\frac{656}{600} + \frac{10 \times 500}{6} \left( 2 + 1 \right) + \frac{8 \times 300}{6} \left( 2 - 1 \right)$ 

1 3.1

54 6

 $B_{1} = B_{3} = 3556 \text{ mm}^{2}$ 

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Direct Stress in Idealized Structure

1. A Juseloge Section as shown in figure Subjected to a bending moment of 100 kNm applied in the vertical place of Symmetry. If the Section has been completely idealized into a combination of direct stress Carrying booms and stead stress only Gringing panets, determine the direct Stress in each boom.



 $M_{n} = 100 \text{ kNm}$   $M_{y} = 0$  The section is Symmetrical to y axis,  $\therefore G_{My} = 0$   $\mathcal{O} = \left(\frac{M_{y} G_{NX} - M_{x} G_{My}}{G_{NX} G_{y} - G_{y}^{2}}\right) x + \left(\frac{M_{x} G_{y} - M_{y} G_{y}}{G_{XX} G_{y} - G_{y}^{2}}\right) y$   $= \frac{M_{x} G_{yy}}{G_{YX} G_{yy}} x y$  M

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			-	and the second second second	
Booms Area mm	y mm	h Yor Inn 4-7 ma	I've mmt		
icade go	640 640	1200	662	280×104	+
4	100 600	1140	602	217× 106	
3	600 600	960	422	106×106	
4	5-20- 600	768	230	312100	
5	640 620	565	27	0.4× 102	
4	640 640	336	- 202	26× 104	
7	850 640	14.4	-394	99× 104	
8	6000 850	38	- 500	212 × 106	
7	8550 640	0	- 538	185×106	
D D	640 850	38	- 500	212×104	
12	Kap 110	144	-394	99×106	
13	620	565	-202	26× 106	
14	600	768	27	04×106	
16	600	960	4 22	31× 106 106× 106	

 $\overline{Y} = (640 \times 1200) + (600 \times 1140) + (600 \times 960) + (600 \times 768) + (620 \times 565) + (640 \times 336) + (640 \times 144) + (850 \times 38) + (640 \times 0) + (850 \times 38) + (640 \times 144) + (640 \times 336) + (620 \times 565) + (600 \times 768) + (600 \times 768) + (600 \times 760) + (600 \times 1140)$ 

640+ 600+ 600+ 620+ 640+ 640+ 850+ 640+ 850+

640+640+620+600+600+600

 $\bar{y} = \frac{5589200}{10380} = 538 \text{ mm}$ 

$$\frac{G_{NK_{1}}}{G_{NK_{1}}} = \frac{bol^{2}}{h^{2}} + A_{1}k_{1}^{2}$$

$$\frac{G_{NK_{1}}}{G_{NK}} = \frac{G_{NK_{1}}}{G_{NK_{1}}} + \frac{G_{NK_{2}}}{G_{NK_{1}}} + \frac{G_{NK_{2}}}{G_{NK_{2}}} + \frac{G_{NK_{2}}}{G_{NK_$$

$$G_{4}^{c} = \frac{100 \times 10^{4}}{1847 \times 10^{4}} \times -202$$

$$= -10.9 \text{ N/mm}^{1}$$

$$G_{7}^{c} = \frac{100 \times 10^{4}}{1847 \times 10^{4}} \times -394$$

$$= -\alpha 1.3 \text{ N/mm}^{2}$$

$$G_{8}^{c} = \frac{100 \times 10^{4}}{1847 \times 10^{4}} \times -500$$

$$= -27.05 \text{ N/mm}^{2}$$

$$G_{7}^{c} = \frac{100 \times 10^{4}}{1847 \times 10^{6}} \times -538$$

$$= -29.1 \text{ N/mm}^{2}$$
By Symmetry (cross section is Symmetrical to y axis)  

$$G_{4}^{c} = G_{16}^{c} = 32.5 \text{ N/mm}^{2}$$

$$G_{5}^{c} = G_{15}^{c} = 22.8 \text{ N/mm}^{2}$$

$$G_{5}^{c} = 0.5 \text{ N/mm}^{2}$$

$$G_{5}^{c} = 0.5 \text{ N/mm}^{2}$$

$$G_{7}^{c} = 0.9 \text{ N/mm}^{2}$$

J. Calculate the shear flow distribution in the Channel Section shown in fig. produced by a vertical shear load of 4.8 kN acting through its shear Centre. Assume that the walls not the section are only effective in resisting Shear Stresses justile. The booms, each of area 300 mm² coning all direct Stresses. 4.8 KN 200mm 14 210 6000 - 50000 - COO K 200 mm = 12 000 000 2005 . 2005 . 005 3 8 = 4.8×1000 ( Sy = 4800 N 0.45 × 005 × 240 - 4500 1113800000001 : The Section is Symmedrical to one 0000000 = 5 JAN mindia des i 9 = - Sy Iyy non Aiyi on

Hearth 1 2 = - Sy A: y: dy . It gender Area Booms x Axit Ay all 300 1 est? 2000 400 60000 60000 200 300 othe 200 2 0 60000 200 0 -60000 300 0 1900 -200 3 0 60000 - 60000 - 400 4200 300 4 = 300x 200<sup>2</sup> 1200 = 12 000 000 mm4 = 12:000 000 mm4 = 12000000 mm 4  $\begin{aligned}
& 9_{12} = -\frac{4800}{46898000} \times 300 \times 200 & (1-1) \times 100 \times (200)^{2} \\
& = -6 \times / \text{mm} \\
& = -6 \times / \text{mm}
\end{aligned}$ = 12000000 mm4 9/23 = -4800 × 309×200 = -6 + 9/2 = -12 N/mm

Shoar glow distribution in idealized structures. · Calculate the shear ylow distribution in the Channel Section shown in fig: produced by a valical stead load of 1 kn. Assume too the walks of the Section are only effective in stesisting shear Stress while the booms Coxy all direct stress. 2m2 D 9 4 m2 16 - 201 10 10 - A 111.336 10 m y of Angein Ay Booms of Aven n 0 0 0, 0 4 A 2 10/10/11/20 0 B 0 180 -(F 2 | 5 Deer) -0 30 0 0- (5:88- x0001) sc g 1 10 30 20 60 π===<u>EAn</u> = <u>40</u> = 52.853m EA - 14 

$$\sum_{N=0}^{\infty} A_{N} = \begin{cases} k_{N}^{10} T_{N} \\ y - y \\ y - y \\ y - y \\ y - y \\ x -$$

N.S.

$$\begin{aligned}
\int_{AB} = (-0.098 \times 4 \times - 2.857) + (-0.326 \times 4 \times -17.142) \\
&= 23.473 \ n/m \\
\int_{Bc} = (-0.098 \times 2 \times 7.143) + (-0.326 \times 2 \times -17.142) \\
&+ 2n_B \\
&= 33.29 \ n/m \\
\int_{CD} = (-0.098 \times 2 \times 7.143) + (-0.326 \times 2 \times 12.858) \\
\int_{CD} = (-0.098 \times 2 \times 7.143) + (-0.326 \times 2 \times 12.858) \\
&+ 2n_B \\
&= 23.506 \ n/m \\
&\frac{23.5 \ n/m}{9} \\
&= 23.506 \ n/m \\
&\int_{C} \frac{23.5 \ n/m}{9} \\
&= \frac{23.506 \ n/m}{10} \\
&\int_{C} \frac{23.5 \ n/m}{9} \\
&= \frac{23.506 \ n/m}{10} \\
&\int_{C} \frac{23.5 \ n/m}{10} \\
&\int_{C}$$

91.h

Shear glow in Closed Section beam.  $9 = \frac{S_y I_{ny} - S_n I_{nn}}{I_{nn} I_{yy} - I_{ny}} A_{ix_i} + \frac{S_n I_{ny} - S_y I_{yy}}{I_{nn} I_{yy} - I_{ny}} A_{iy_i} + \frac{9}{2_{s,s}}$ The moment of the Section will be balanced at The open Section when it is closed? 10 T= QA 25,01 1. A thin walled Single Cell beam Shown in Fig. has been idealized into a Combination of direct stress awying booms and shear stress only awying walls. If the section supports a vertical shear had of 10 km acting in a vertical plane. the shear I to km acting in a vertical plane. through booms 3 & 6, Calculate the Shear low distribution around the section. Borden areas.  $B_1 = B_8 = 200 \text{ mm}^2$ ,  $B_2 = B_7 = 250 \text{ mm}^2$ ,  $B_1 = B_2 = 1000 \text{ mm}^2$ ,  $B_2 = B_7 = 250 \text{ mm}^2$ ,  $B_2 = 250 \text{$  $B_3 = B_6 = 400 \text{ mm}^2 B_4 = B_5 = 100 \text{ mm}^2 0 000$ 2 100011 001- 10KN 0 0008. 0 0 6.14 seting out - 3 opport 60 mm 0 d 1000 M S 01-000 120mm 240 240 00.1

12 A Q.

$$2 = \begin{bmatrix} s_{y}T_{ny} - s_{y}T_{ny} \\ F_{nx}F_{yy} - F_{ny} \end{bmatrix} A_{1}x_{1} + \begin{bmatrix} s_{y}F_{ny} - s_{y}T_{yy} \\ T_{ny}T_{yy} - T_{ny}T_{yy} \end{bmatrix} A_{1}y_{1} + g_{2},$$

$$A_{1}y_{1} + g_{2},$$

$$A_{2}y_{1} + g_{3},$$

$$A_{2}y_{1} + g_{3},$$

$$P = \frac{-s_{y}T_{yy}}{T_{nn}T_{yy}} = A_{1}y_{1} + g_{3},$$

$$P = \frac{-s_{y}}{T_{nn}T_{yy}} = \frac{-s_{y}}{T_{ny}} = 100 \text{ mm}$$
$$\begin{aligned} f_{1x} &= \xi_{A}\chi^{2} \\ &= 13860 \ 60 \ 0 \\ f_{mx} &= 13.86 \ \chi 10^{6} \ mmt \\ \\ & & & & \\ &$$

1 281 = 9 = -18.03 N/mm The moment at any point of the Section will be balanced when it is closed.

T = &A 9 ...

take moment about the intersection of Shear hand and One of Symmetry, Restrayedy

 $\begin{array}{c} 2_{518} \times 60 \times 480 + 9_{431} \times 240 \times 100 + 9_{387} \times 240 \times 30 \\ + 9_{23} \times 240 \times 100 + 9_{76} \times 240 \times 100 \\ - 9_{434} \times 120 \times 100 - 9_{56} \times 190 \times 120 = 0 \\ - 9_{45} \times 100 \times 120 = 0 \\ \end{array}$ 

to find Avea,

$$A = \left( (120 \times 50) + \left( \frac{1}{2} \times 120 \times 50 \right) + \left( 240 \times 100 \right) + \left( 2240 \times 70 \right) + \left( 30 \times 240 \right) \right) \times 2$$

: A = 97200 mm

Take moment with respect to any point on the beam to find T and substitute in the above equation to find qs0 Add qso with all the basic shear flow values.

Unit IV Analysis of Aircraft Component. Stress Fuse lages: a Bending " The Juse lage of a lighter passenger Carrying aircraft has the circular section shown in Fig. and the Cross - Sectional area of each Stringer is 100mm<sup>2</sup> and the vertical distance given in fig. are to sthe mid line of the Section wall at the corresponding Stringer Position. If the Juse lage is subjected to a bending moment of 200 KNM applied in the vertical plane of Symmetry, at this section, Calculate the direct stress distribution.  $B = \frac{tb}{c} \left( 2 + \frac{5}{5} \right)$ + = 0.8 mm

 $b = \frac{2\pi r}{16} = \frac{2 \times 3.14 \times 3.81}{16} = 14.9.6 \text{ mm}$ 

$$B_{1} = 100 + \frac{0.8 \times 147.6}{6} \left( 2 + \frac{\sigma_{2}}{\sigma_{1}} \right) + \frac{0.8 \times 147.6}{6} \left( 2 + \frac{\sigma_{1}}{\sigma_{1}} \right)$$
$$= 100 + \frac{0.8 \times 147.6}{6} \left( 2 + \frac{352}{381} \right) + \frac{0.8 \times 147.6}{6} \left( 2 + \frac{352}{381} \right)$$
$$= 100 + 58.244 + 58.244$$

 $\odot$ 

$$B_{3} = 100 + \frac{0.8 \times 14.7.6}{6} \left( 2 + \frac{\sigma_{3}}{\sigma_{2}} \right) + \frac{0.8 \times 14.7.6}{6} \left( 2 + \frac{\sigma_{1}}{\sigma_{2}} \right)$$
$$= 100 + \frac{0.8 \times 14.7.6}{6} \left( 2 + \frac{36.9.5}{3.52} \right) + \frac{0.8 \times 14.7.6}{6} \left( 2 + \frac{3.81}{3.52} \right)$$
$$= 100 + 15.26 + 0.46$$

$$B_{1} = 216 \text{ mm}^{2}$$

$$B_{3} = 100 + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{\sigma_{4}}{\sigma_{3}} \right) + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{\sigma_{5}}{\sigma_{3}} \right)$$
  
= 100 +  $\frac{0.8 \times 149.6}{6} \left( 2 + \frac{145.8}{269.5} \right) + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{352}{269.5} \right)$ 

$$B_3 = d/6 mm^2$$

$$B_{4} = 100 + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{\sigma_{5}}{\sigma_{4}} \right) + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{\sigma_{5}}{\sigma_{4}} \right)$$
  
= 100 +  $\frac{0.8 \times 149.6}{6} \left( 2 + \frac{0}{145.8} \right) + \frac{0.8 \times 149.6}{6} \left( 2 + \frac{369.5}{145.8} \right)$ 

= 100 + 39.88 + 76.73

 $B_q = 216 \text{ mm}^2$ 

3.  

$$B_{5} = 100 + \frac{0.18 \times 147.6}{6} \left( 2 + \frac{S_{5}}{S_{5}} \right) + \frac{0.18 \times 147.6}{6} \left( 2 + \frac{S_{7}}{S_{5}} \right)$$

$$= 100 \text{ mm}^{2} + 4.464.4$$

$$B_{1} = B_{2} = 3.2 \text{ and } \frac{1}{2}$$

$$B_{3} = B_{3} = 3.6 \text{ mm}^{2}$$

$$B_{4} = B_{4} = B_{5} = B_{10} = 2.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$B_{5} = B_{5} = 100 \text{ mm}^{2} + 4.66 \text{ mm}^{2}$$

$$D_{10} d \text{ Ships} = \frac{0}{100 \text{ mm}^{2} + 4.666 \times 351.0^{2}} + 4.6 \times 24.6 \times 24.6$$

		, OP		
Booms	Aven	Ĩ	Inn (10")	03 6
្ន	216	381	31	314
2	216	352	36	290
3	216	269.5	15	222
4	216	14 5.8	4	120.49
\$	216	0	. 0	0
6	216	-14.5.8	4	-120.49
۲	211	- 2 67.5	15	-222
8	216	-352	26	-290
9	216	- 381	31	- 314
10	216	352	26	-290
11	316	- 269.5	15	The I was a
12	211	-145.8	4	-222
13	216	0	0	-120.49
14	216	145.8	K- aM	0
12	حدال	269.5	15	222
16	216	352	26	290
			2. 4	

$$\frac{g_{1x}}{f_{1x}} = \xi A L^{2}$$

$$= 242 \times 10^{6}$$

$$= 2.42 \times 10^{8} mm^{4}$$

$$M_{x} = 200 \text{ KN-m}$$
  
= 200 x 10<sup>3</sup> Nm  
= 200 x 10<sup>6</sup> N-mm

elage Shear Problem. The jusclage of a light possenger carrying aircraft has the Circular Cross section Shown in sig. The cross sectional area of each stringy is 100mm² and the vertical distance given in Fig. are to the mid line of the Section wall at the corresponding stringer position. If the 10 Subjected to a vertical shear load of 100 km applied at a distance of 150 mm from The vertical aris of Symmetry as shown Glaulate the distribution of show ylow, Som 8  $B = \frac{tb}{t} \left( a + \frac{\sigma_2}{\sigma_1} \right)$ t = 0.8 mm  $b = 2\pi Y = 2 \times 3.14 \times 381$ 

= 149.6mm

$$\begin{split} B_{1} &= 100 + \frac{0.8 \times 143 \cdot L}{4} \left( \frac{1}{4} + \frac{\sigma_{1}}{\sigma_{1}} \right) + 0.8 \times \frac{143 \cdot L}{4} \left( \frac{1}{4} + \frac{352}{351} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{351} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{351} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{351} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{351} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{352} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{351}{352} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{351}{352} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{381}{352} + \frac{352}{2} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{351}{352} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{351}{352} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{353}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \left( \frac{1}{4} + \frac{352}{227} + \frac{0.8 \times 143 \cdot L}{4} - \frac{1}{4} - \frac{1}{4} + \frac{0.8 \times 143 \cdot L}{2} - \frac{1}{4} - \frac{1}{4} + \frac{0.8 \times 143 \cdot L}{4} - \frac{1}{4} - \frac{1}{4} + \frac{0.8 \times 143 \cdot L}{4} - \frac{1}{4} - \frac{1}{4} - \frac{1}{4} + \frac{0.8 \times 143 \cdot L}{4} - \frac{1}{4} - \frac{$$

and the second sec

°,

$$B_1 = B_q = 2/6 \text{ mm}^2$$

$$B_2 = B_{16} = B_8 = B_{10} = 2/6 \text{ mm}^2$$

$$B_3 = B_{15} = B_7 = B_1 = 2/6 \text{ mm}^2$$

$$B_4 = B_{19} = B_6 = B_{12} = 2/6 \text{ mm}^2$$

$$B_5 = B_{13} = \text{unleft}$$

?

bovieslan flow,  

$$\begin{aligned}
& \beta_{k} = \begin{bmatrix} S_{y} \leq n_{y} - S_{u} \leq n_{k} \\ \exists n_{u} \leq s_{y} - S_{u} \end{bmatrix} A_{i} n_{i} + \begin{bmatrix} S_{u} \leq n_{u} - S_{u} \leq s_{y} \\ \exists n_{u} \leq s_{y} - S_{u} \end{bmatrix} A_{i} y_{i}; \\
& S_{n} = 0, \quad T_{ny} = 0 \\
& \beta_{k} = 0 + \begin{bmatrix} -S_{y} \leq s_{y} \\ \exists n_{u} \leq s_{y} \end{bmatrix} A_{i} y_{i}; \\
& \beta_{k} = -\frac{S_{y}}{\sum n_{u}} A_{i} y_{i}; \\
& fold \quad Sheau \, ylow, \\
& g = \beta_{k} + \beta_{k}, o
\end{aligned}$$

2 .

44.7

A AS

A 260 1

Open Booms 9 mm Avea 35 z 269.5 145.8 wdefind -145.8 -269.5 -352 -381 -35z - 269.5 -145.8 undefinal 145.8 .4. 269.5 

Inn = EAL = 242 × 106  $= 2.42 \times 10^8 \text{ mm}^4$ 

Open panned 1-2

V12 :0

$$= \frac{-100 \times 10^{3}}{2.42 \times 10^{8}} \times 2.16 \times 3.52$$
  
= - 31 N/m

$$\frac{9}{7_{34}} = -\frac{5y}{I_{nm}} A_{i} y_{i}^{*} + \frac{9}{7_{23}}$$
$$= -\frac{100 \times 10^{3}}{2 \cdot 4^{2} \times 10^{8}} \times 216 \times 269 \cdot 5 + \frac{9}{7_{23}}$$

$$= -68 \, \text{N/mm}$$
 of (-55)

$$7_{56} = 0 - 68 \, \text{N/m}$$
  
= -68 \mess/mm.

Here .

$$\begin{aligned} g_{17} &= -\frac{100 \times 10^{3}}{2.42110^{6}} \times 2.16 \times -145.8 + 9_{51} \\ &= 12.97-68 \\ &= -55 \, \text{N/mm} \end{aligned}$$

$$\begin{aligned} &\overline{9}_{78} &= -\frac{100 \times 10^{3}}{2.42110^{8}} \times 2.16 \times -269.5 + 9_{62} \\ &= -31 \, \text{N/mm} \end{aligned}$$

$$\begin{aligned} &\overline{9}_{89} &= -\frac{100 \times 10^{3}}{2.42 \times 10^{8}} \times 2.16 \times -352 + 9_{78} \\ &= 31 - 31 \\ \hline 9_{89} &= 0 \end{aligned}$$

$$\begin{aligned} &\overline{9}_{174} &= -\frac{100 \times 10^{3}}{2.42 \times 10^{8}} \times 2.16 \times 381 &\neq \\ &\overline{9}_{1.42} &= -33 \, \text{N/mm} \end{aligned}$$

$$\begin{aligned} &\overline{9}_{1.6-5} &= -\frac{100 \times 10^{3}}{2.42 \times 10^{8}} \times 2.16 \times 352 - 33 \\ &= -64 \, \text{N/mm} \end{aligned}$$

$$\begin{aligned} &\overline{9}_{15-14} &= -\frac{100 \times 10^{3}}{2.42 \times 10^{8}} \times 2.16 \times 367.5 - 64 \\ &= -23.9 - 64 \\ &= -23.9 - 64 \\ &= -8.8 \, \text{N/mm} \end{aligned}$$

$$\frac{4}{2}$$

$$\frac{1}{2}$$

$$\frac{1}$$

$$T = 2A \frac{1}{25,0}$$

$$A = \pi \times 381^{2}.$$

$$= 455 \times 10^{5} \text{ mm}^{2} \qquad \text{moves here } \left\{2 \times \frac{1}{14}\right\}^{1/4} + \frac{1}{24} \times \frac{1}{14} + \frac{1}{24} \times \frac$$

T = 5431737.25

 $\left\{ \begin{array}{c} \cdot \\ \cdot \\ \end{array} \right\} q_{s,0} = \frac{T}{2A} \right\}$ 

9.5,0	1	5431737.25
		ax 4560367

15,0 = 5.955 N/MM

The12 = 5.955 9623 = - 30.29+ 5.955 = -24.33 N/mm 9/1834 = - 53.48 + 5.955 = -47.525 N/mm 945 = -66.02 + S.955 = -60.065 NIMM -66.02 + 5.955 = - 60.065 NIMM 21556 Ξ = -53.48 + 5.955 = - 47.525 NIMM 91067 2078 = -30.29 + 5.955 = -24.33 NIMM 989 = 5.955 NIMM 9910 32.7+5.955 = 38.655 NIMM Ξ = 63+5.955 = 68.955 N/mm Tion 92.145 N/mm = 86.19 + 5.955 = 9112 98.7 + 5.955 = 104.665 NIMM 21013 Ξ 104.665 N/mm 98.7 + 5.955 = 91314 2 85.9 + 5.955 = 91.855 NIMM 91415 : 62.7 + S.955 = 68.6 XIMM 91516 Ξ 31.7 + 5.955 = 37.655 N/mm. 9161 =

wing Section shown in fig has been idealized such that the booms carry all the direct strusses. If the wing section is subjected to a bending moment of. 300 kNM applied in a verifical plane, Calculate the direct strusses in the booms.

 $(\mathbf{r})$ 



Boom areas:  $B_1 = B_6 = -2580 \text{ mm}^2$   $B_2 = B_5 = 3880 \text{ mm}^2$  $B_3 = B_4 = 3230 \text{ mm}^2$ 

Guilen datat

Sof

 $M_{y} = 0$   $M_{x} = 300 \text{ kNm} = 300 \times 10^{6} \text{ Nmm}$   $I_{xy} = 0 \quad [:: \text{ distribution of boom areas is Symmetrial} about x - axis]$   $\sigma = \frac{M_{x}}{I_{xx}} y$ 

$$\sigma = \frac{300 \times 10^6}{I_{XX}} y$$

				A state of the sta	
Booms	area	y	Ayx103	I INX XIDE	
1	2580	165	425.7	70	
2	3880	230	892.4	2.05	·
3	3230	200	646	129	
Ч	3230	- 200	-646	129	
5	3880	- 230	- 892.4	205	
b	2580	-165	-425.7	70	

 $I_{xx} = 808 \times 10^6 \text{ mmy}$ 

Robling

The wing section shown in fig Carries a vertically upward shear load of 86.8kN in a plane of use 572. The section has been idealised such that the booms results all the direct stresses while the walls are effective only in shear. If the shear modulus of the wall is 27600 mm<sup>2</sup>. Calculate the shear flow distribution the section and the state of turist.



	wall	length (mm)	Hhickness (mm)	Cell avea (mm²)
4	1-2,5-6	1023	1,22	A1 = 265000
	3-4 4-8-3	2200 400	2.03 2.64	$f_{\bar{\Pi}} = 213000$ $f_{\bar{\Pi}} = 413000$
	5-7-2	460	2.64	
	6-1 7-8	330	1.63	5 <b>8</b>
	Boo	m Ateas, B, B	$= B_{0} = 2580 \text{ mm}$ = B = 3230	$B_{1} = B_{5} = 3880 \text{ m}$
84:	Guillen	data;-	5 04 2	

Booms	Area	1 4		Jyz = f	292
	2580	165	11.1	* +0	de
2	3880	230		205	
3	3230	200		129	
ч	3230	-200	×	129	
5	3880	-230		205	
6	2580	-165		-70	

In = 808 × 10° mmy Q6 = -Sy Aiy Ixx " $q_{b} = 0$  at each cut  $Q_{12} = Q_{23} = Q_{34} = 0$ 96,16 = -86-8×103 × 2580 × 165 808×106 9616 = -45-6N/mm  $9_{6,65} = -\frac{86.8 \times 10^3}{808 \times 10^6} \times 2580 \times (-165) + 9_{6,16}$ 96765 = 45.6 - 45.6 = ON/MM  $V_{b,57} = \frac{-86 - 8 \times 10^3}{80 \% \times 10^6} \times 3880 \times (-230) + 0$ N6,57 2 95.86 N/mm 9/6,27 = -86.8 × 103 × 3880× 230 ROB XIDE 96,27 = -95,86N mm  $9_{6,38} = -86.8 \times 10^{3} \times 3230 \times 200$ 808 × 16° 96,38 = -69.39 Nmm 96,48 = - 86-8×103 × 3230× (-200) 808×106 2 69.39 N/mm  $0 = \frac{1}{2AG} \cdot \frac{\gamma}{t} ds$ 

$$\begin{cases} \varphi & \text{Settion} - \underline{1} \\ \varphi & \gamma & 9 65000 \times \gamma & 9 600 \\ \hline \\ \theta_1 & = \frac{1}{2 \times \gamma & 9 65000 \times \gamma & 9 600} \\ \hline \\ \frac{q_{1,01}}{2 \times 2} & \chi & 2200 \\ \hline \\ \frac{q_{1,01}}{2 \times 2} & \chi & 2200 \\ \hline \\ \frac{q_{1,01}}{2 \times 2} & \chi & \frac{q_{1,01}}{2 \times 64} \\ \hline \\ \varphi_1 & = \frac{1}{2 \times 213000 \times 23600} \\ \hline \\ \frac{q_{1,01}}{2 \times 213000 \times 23600} \\ \hline \\ \frac{q_{1,01}}{2 \times 64} & \chi & \frac{q_{1,01}}{2 \times 64} \\ \hline \\ \varphi_{1,02} & \chi & 1200 \\ \hline \\ \varphi_{1,02} & \chi & 100 \\ \hline \\ \varphi_{1,02} & \chi &$$

Let  

$$0_{1} = 0_{2}$$

$$\exists \cdot q_{6} \times i \overline{0}^{3} q_{sol} + i 6 \cdot 3 \times i \overline{0}^{8} q_{sol} = 0 \cdot 5 \exists \times i \overline{0}^{3} q_{sol}$$

$$\xi = 0_{3}$$

$$= 0 \cdot 4_{8} \times i \overline{0}^{3} q_{sol} + 16 \cdot 4 \times i \overline{0}^{8} q_{sol} + 8 \cdot 4 \otimes x i \overline{0}^{3} q_{sol}$$

$$\xi \text{ we leaved that}$$

$$T = -24 \times 10^{3}$$
Solving Eqn @ S & C  

$$q_{sol} = -21 \cdot 47$$

$$q_{sol} = -20 \cdot 41$$
Add these values to the basic shear flow values  

$$\frac{1}{16} \frac{1}{6} \frac$$

P12 Pz1 and Pz2 are the components in the z direction of the axial loads P1 and P2 in the flangs and Py1 and Py2 are the components parallel to y axis.

P2

 $Sy = Syw - P_{31}P_{11} - P_{32}P_{12}$   $P_{31} = \sigma_{31} \times B_{11}, \quad P_{32} = \sigma_{32} \times B_{22}$   $P_{11} = \frac{\delta_{11}}{\delta_{32}}, \quad P_{12} = \frac{\delta_{12}}{\delta_{32}}$ 

Bobleur, - Determine the shear flow distribution in the web of the tapered beam shown in fig. at a section mid way along its jength. The web of the beam has a thickness of smm & fits is fully effective in gresisting direct stress. The beam tapered symmetrically about its hosisontal axis & xooss-sectional area of the boom is 400mm<sup>2</sup>. The internal bending moment is the shear load at the mid section is applied externally.



Gliven Data :-

 $S_{yw} = -20 \text{KN} = -20 \times 10^3$ 

$$S_{3} = 0$$
  
 $J_{3\gamma} = 0$   
 $\delta_{\gamma_{1}} = 100$   
 $\delta_{\gamma_{2}} = -100$   
 $\delta_{3} = 2000$ 

	S	, = Syω-	Pa, Py, - 1	D3, PY2	
•	9	$= -\frac{Sy}{J_{33}}$	1111		
	Pyi	$= \frac{\delta^{41}}{\delta_8}$	100	= 0.05 ^	J
	Py2	= 54.	- 100	= - 0.09	5 N
	Pa,	= 03, X	B, /	$P_{a_1} = \sigma_a$	3° X B°
	53	$= \frac{N_3}{T_{33}}$	- • 7	{ My=0	$M_{2} = 20 \times 10^{3} \times 10^{3}$ $M_{2} = 20 \times 10^{6} N [mm]$
B	DOW	Area	V	A. 8-	Tri (112
1	L	400	150	Ah 9000000	$L33 = \xi A h^{-1}$
1	2	400	-120	9000000	$= 18 \times 10^6  \text{mm}^4$
	*	0 <sub>31</sub> = .	20×10 <sup>6</sup> 18×10 <sup>6</sup> X	150 = 1	66.6 N/1mm2
ι. Έλ		032 =	20× 10° × 1	(-150) = -	-166.6 N/mm=
	-	Pa1 =	166.6 x 4 0	00 = 66	640 N
		P32 =	- 166.6 %	400 = -	66640N
ί.	\$	3y = - ;	$20 \times 10^3 - ($	666.40 X O	·05)-(-66640x (0.05))
		Sy = -	26664N		M.
		912 =	-SY A	141	
		912 =	-133 26664 18×10	χ μοο X	1500 - 10021
		912 =	88.8	N)mm.	et l'a to the

2 cell beau hers singly symmetrical moss-sections, 1.2 m a path & tapens symmetrically in the y-direction about a longitudinal axis . The beaus supports load which produces a shear force of lokal in y-direction & bending moment Mx of 1.65 KNI-M et a larger cross-section the shear load is applied in the plane of internal spar web 97 the booms I & G lie in a plane which is parallel to 43 plane, culculate the Force In the booms & then shew Flow distribution for the walls at the larger X-section. the booms are assumed to mestst all the dimet stresses while the wells are effective only in shear the shear module is constant throughout the vortical - webs are 1mm thickness achile the gremaining will are 0.8 mm thick.

BOUNDER IN PERSONAL PROPERTY IN THE REPORT Larver John He Las PerMy 510 192-501 12635 107-94 171-2 2534 111.1. \$ 20 01-W. Fart - 'Ll) UNEL APPAL 11784 ---

		Boon	ns Arrea			617.5		d to		
		B1=	B3 = Bc	1 = E	36 = 600 r	nn²				
		B2:	= B5 =	900	smu2		i capital			
		Sta	= loki	J =	10 × 13 N			in survey.		
	te f	Mx	= 1.65	KN-1	4 = 1.6	5 X 10	Nm	m		2
		Sz	5 1.21	n =	1200 mm	$e \hat{x} = -i \hat{x}$	ta e	5 6 4		
			an a an	5 eft	a) 234		1 62.	da dari		1 1
			130	11-	2-11-	1.00	01 814 	and a set of	t 24 To had	
		k i nac	180	O			ber i k Stada	As a	and all	
		i ann	4	200	100			a Aria ta	· 1;	hasten :
			,							
			- ) <sup>4</sup> (ve	of in	m & C att	e dha		I. M. Maria	5 44	ations
Booins	Areq	σ,	$P_{Y} = \frac{\delta Y}{\delta 3}$	H IN	Ah- XIOC	Ixx= End	σx	PL=GxB	Pe x Py	έBepy
Booms	Areq 600	50	$P_{Y} = \frac{\delta Y}{\delta 3}$ 0.041	४ व0	$Ah^2 \times 10^6$ $4.8 \times 10^6$	Txx= {ak	σ <del>χ</del> 4-39	PL=GXB 2634	Be x Py 107+99	ÉREPY
Boours 1 2	Area 600 900	50 02	$P_{1} = \frac{\delta y}{\delta 3}$ $0.041$ $0.041$	४ १० १०	Ah- x10 <sup>6</sup> 4.8 × 10 <sup>6</sup> 7.29 ×10	Ixx= fak	07 4-39 4-39	PL=GXB 2634 3951	Px x Py 107.99 161.99	έRepy
Booms 1 2 3	Areq 600 900 600	20 20 20 20	$P_{Y} = \frac{\delta Y}{\delta 3}$ $0.041$ $0.041$	भ व० व० व०	Ak- ×10° 4.8 × 10° 7.29 ×10° 4. 59 ×10°	Ixx = { ak 5.3. W 901 X 80	07 4-39 4-39 4-39	PZ=65×B 2634 3951 2634	Px x Py 107,99 161,99 167,99	E P2 Py to:s
Booms 1 2 3 4	Areq 600 900 600 600	- 20 03	$P_{Y} = \frac{\delta Y}{\delta 3}$ $0.041$ $0.041$ $0.041$ $-0.041$	у 90 90 -90	Ak- ×10° 4.8 × 10° 7.29 ×10° 4.88 ×10°	Ixx = { at 5 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	07 4-39 4-39 4-39 -4-39	PZ=63×B 2634 3951 2634 -2634	Px x Py 107.99 161.99 107.99 107.99	ER2Py hb.sst
Booms 1 2 3 4 5	Areq 600 900 600 900	-20 02 03- 03-	$P_{Y} = \frac{\delta Y}{\delta 3}$ $0.041$ $0.041$ $-0.041$ $-0.041$	У 90 90 -90 -90	Ak- ×10° 4.8 × 10° 7.29 ×10° 4.88 ×10° 4.88 ×10° 4.88 ×10°	Txx= fak 5-3-3-2 8 X 10 8 3-1 8 3-1 8 5-1 8 5-1 8 5-1 1-1 1-1 1-1 1-1 1-1 1-1 1-1 1-1 1-1	07 4-39 4-39 4-39 -4-39 -4-39	Pz=65×B 2634 3951 2634 -2634 -3951	Px x Py 107.99 161.99 107.99 107.99	ER2Py Ho-SSE

$$S_{Y} = S_{YW}^{-} \geq P_{X} P_{Y}$$

$$S_{Y} = 10 \times 10^{3} - 755.94$$

$$S_{Y} = 9244.06 \text{ N}$$

$$- Q = -\frac{S_{Y}}{I_{XQ}} A_{1}Y_{1}^{-}$$

•

$$-\frac{q_{2}u_{1}u_{2}}{q_{3}} \times 10^{5} \times 100 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$H_{15} = -\frac{q_{2}u_{1}u_{5}O}{q_{3}} \times 10^{5} \times 100 \times q_{0} = -22.16 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{1}u_{5}O}{33.78 \times 10^{5}} \times 200 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{1}u_{5}O}{33.78 \times 10^{5}} \times 200 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{5}G}{33.78 \times 10^{5}} \times 200 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{5}G}{33.78 \times 10^{5}} \times 200 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{5}G}{33.78 \times 10^{5}} \times 200 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{5}G}{33.78 \times 10^{5}} \times 2000 \times q_{0} = -14.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{q_{2}u_{5}G}{33.78 \times 10^{5}} \times 2000 \times q_{0} = -10.77 \text{ N/Jmm}$$

$$Q_{15} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{4} \cdot d_{5}$$

$$Q_{1} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{400} + \frac{q_{15}T}{1} \times 100 + \frac{q_{15}T}{0.8} \times 1000 + \frac{q_{15}T}{1} \times 100}$$

$$Q_{1} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{0.8} - 2.5 \times 10^{5} \frac{q_{15}T}{1} - 0$$

$$A_{10} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{0.8} - 2.5 \times 10^{5} \frac{q_{15}T}{1} - 0$$

$$A_{10} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{0.8} - 2.5 \times 10^{5} \frac{q_{15}T}{1} - \frac{q_{15}T}{1} \times 100 + \frac{q_{15}T}{0.8} \times 1000 + \frac{q_{15}T}{1} \times 100}$$

$$Q_{1} = -\frac{1}{2000} \times 10^{5} \frac{q_{15}T}{0.8} + \frac{q_{16}u_{1}}{0.8} \times 10^{5} \frac{q_{15}T}{1} - \frac{q_{15}}{1} \times 1000 + \frac{q_{15}T}{1} \times 1000}$$

$$Q_{1} = -\frac{1}{200} \times 10^{5} \frac{q_{15}T}{0.5} + \frac{q_{16}u_{1}}{0.8} \sqrt{10^{5}} \frac{q_{15}T}{0} - \frac{q_{15}}{0}$$

$$Q_{1} = -\frac{1}{200} \times 10^{5} \frac{q_{15}T}{0.5} + \frac{q_{16}u_{1}}{0.8} \sqrt{10^{5}} \frac{q_{15}T}{0} - \frac{q_{15}}{0}$$

$$Q_{1} = -\frac{1}{20} \times 10^{5} \frac{q_{15}T}{10} + \frac{q_{16}u_{1}}{0.8} \sqrt{10^{5}} \frac{q_{15}}{0} = \frac{q_{16}}{0} \times 10^{5} \frac{q_{16}}{0} = \frac{q_{16}}{0} \times 10^{5} \frac{q_{16}}{0} = \frac{q_{16}}{0} \times 10^{5} \frac{q_{16}}{0} = \frac{q_{16}}{0} \times 100 \times 100$$

$$T = -\frac{q_{16}}{0} \times 100 \text{ N-mm}$$

T

2. . . .

Unit V <u>Energy</u> Methods: strain energy due to axial, bending and Torsional loads - Castigliano's theorem

Strain energy (or) Resilience: When the elastic body is loaded it undergoes deformation i.e. its dimensions change and when it is relieved of the load it regains its original shape. (At the same time, the energy stored in the elastic body is Called as Strain energy. For the time loaded energy is stored in it, the same

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is given up (or) released by the loading when the load is removed. This energy is Called as strain energy. The strain energy stored "within" the elastic limit when loaded externally is called "Resilience", and the maximum energy which a body stores upto" elastic\_limits is called prof resilience". ananjiera (ez) kininera Resilience : The strain energy stored within" the elastic limit, when loaded externally is Called as "Resilience". Part process and e playmente Proof Resilience:  $\alpha x_{P} \cdots = \cdots = \alpha x_{P}$ The maximum energy stored

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within a body "up to" elastic 3 limit is Called as "Proof resilience" Proof redilience is the mechanical property of materials and it indicates their Capacity to bear shocks. Modulies of Resilience: Volume of piece is Called "Modules of resilience". Strain energy in Simple tension and Compression: (Strain energy due to axial load Let us take the Case of a bar of Gross - Sectional area A and length "1" and Subjected

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to a load "W". Suppose this load extends the bar by an amount El and produces a maximum <del>Stress</del> stress, 0. The Workdone by W and hence the Strain energy (U) stored in the material is equal to the area under the force extension Curre. March Catholicae Force (load) W Extension Maggina is Scanned with CamScanne

Strain energy stored in the bar = Work done by the load 1/2. W.S.L 1.81= Wx ol. To X W=OXA  $\sigma^2 V$ where, A => Area E= Modulus of Elasticity 1=) length of bar > Volume of bar T=> stress, be the proof stress (No. W.) 6 W 0 K Scanned with CamScanner

(or) the maximum stress to which the bar is stressed up to the elastic limit, then Proof resilience,  $U_p = \frac{O_p^2}{2E} \times V$ and, modulus of resilience, =  $\frac{O_p}{2E}$ 2-JT QL 5.) A bour of Steel bar of 4 cm by Acm in Section, 3m long is Subjected to an axial full of 128 KN. Taking E= 200 GN/m2. Find the alternation in the length at of the bar. Calculate also the amount of energy stored in the bax during the extension.

Solution: Cross Sectional area of the bar, A = 4 cm × 4 cm = 16 cm<sup>2</sup>  $A = 16 \times 10^{-4} m^2$ 128 KN Acm 28 KN Axial pull applied, W=128KN of the bar = l= 3m. Longth Modulus of elasticity, 200 GIN/m2  $E = 200 \times 10^9 N/m^2$ Elongation of bar, S.l:-(81= Scanned with CamScanner

81 = 128 × 10×3 16×10-4×200×109 SL = 0.0012m (or) 12mm, Energy stored in the bar during elongation,  $U_{1}^{2}$  =  $\frac{W}{A} = \frac{128 \times 10^{3}}{16 \times 10^{-4}}$ 0=16×107N/2 WKT, U= \_\_\_\_ XAL  $U = \frac{(8 \times 10^{7})^{2} \times 16 \times 10^{7} \times 3}{(8 \times 10^{7})^{2} \times 16 \times 10^{7} \times 3}$ 2×200×109 U = 76.8F 5.2) A steel Specifien 1.5 cm² In Cross-Section Stretches 0.05mm over 5cm gauge length under an axial load of 30kr. Calculate the Strain energy

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stored in the specimen (9) at this point. If the load at the elastic limit for specimen is 50 KN. Calculate the elongation at the elastic limit and the resilience. Solution; Grogg-Sectional area of Specimen, A = 1.5 cm²  $A = 1.5 \times 10^{-4} m^2$ Increase in length over 5cm gauge length, SL= 0.05mm 82=0.05×10 m Axial Load, W=30KN=30X10<sup>3</sup>N Load at clastic limits = 50KN, = 50X10<sup>3</sup>N, <del>strain</del> energy stored in specimen, U:- $U = \frac{\sigma^2 A L}{2E} = \frac{1}{2} \cdot W \cdot S L$ 

 $U = \frac{1}{2} \times (30 \times 10^3) \times 0.05 \times 10^3$ = 0.753 Also, |E=3 res Sr A.S 30×103×(5/100) 1.5×154×0.05×10 E = 200 × 109 N/m2 limit, S.L. elastic ongation at 50×103× 100) 00×109 (10

11) SI = 0.000083.3m L = 0.0833 mm5.3) A bar 100 cm in length 13 Subjected to an axial pull, such that the maximum stress is equal to 150 MN/m?. Its area of Gross-Section is 2cm<sup>2</sup> over a length of 95cm and for the middle 5cm length it is only 1 cm?. If E = 200GN/m², Calculate the strain energy stored in bar. Solution.

Maximum stress in portion of 1 cm² Gross-Section, 01=150MN/m2 Maximum stress in portion of 2cm<sup>2</sup> Cross-Section,  $\sigma_2 = 75 \, \text{MN/m}^2$ WRT,  $\sigma_1 A_1 = \sigma_2 A_2$  $150 \times 10^{-4} = 02 \times 2 \times 10^{-4}$  $0_2 = \frac{150}{2} = 75 MN/m^2$ strain energy stored in the bar,  $U = \frac{\sigma_{1}^{2} A_{1} J_{1}}{2E} + \frac{\sigma_{2}^{2} A_{2} J_{2}}{2E}$  $U = (150 \times 10^6)^2 \times (1 \times 10^{-4}) \times (5/100)$ 2×(200×(07) (75×106)2×(2×10 4)× (95/100)

U= 2.953Nm (01) Joules. (5.4) Two Similar bars A and B are each 30cm long as shown in Sigure. The bar A receives an axial blow, which produces a max. maximum stress of 200 MN/m². Find maximax. Stress produced by the same blow on the bar B. If the bar is stressed to 200 MN/m? Retermine the ratio of energy stored by the bars and A and B. 10 cm 20mb 20 cm \$4 cm = 10 cm 20 cm - 74 cmg

Solution: Max. Stress in the bar A (2cm diameter portion),  $\sigma_{I_A} = \sigma_A = 200 \, \text{mN/m}^2.$ : stress in the 4cm diameter portion 2A= 50 MN/m2.  $\sigma_1 A_1 = \sigma_2 A_2$  $200 \times \frac{T}{4} \left(\frac{2}{100}\right)^2 = \sigma_2 \times \frac{T}{4} \times \left(\frac{4}{100}\right)^2$ Max. stress in bar B (2cm dlameter portion), OBI=? Stress in Acm diameter portion  $O_{B2} = \frac{O_{B1}}{B_{B2}}$ 

(according to previous result (15) y stress rA, DO, AI.  $l_2$ 2E 10 (200×106)2× T+× (2 2× x 20 100 (50×10<sup>6</sup>)<sup>2</sup> 100 1E 3TX 10 11 TT X10 TX10 the by tored 20 Sim 2 OB X 10 2E

UB = 2'25 TT OB 2 105×2E barrs A ar Since the blow on the R is the same, therefore the two e are equal. 3TT XID 105X 3×10" ×10 ×2 2.25 N/m  $\sigma_B = 163.3 \text{ MN/m}$ by energy stored Katio of UA VB A and B: Energy stored in bar B when it is also stressed to 200 MN/m. 2.25 TT OB

 $B = \frac{2.25\pi \times (200\times 10^6)^2}{10^6}$ 105×2E 4.57 × 10 11 . Kation 19 A and STX 10 2 00 Kar 4.5TT X 10" energy in pure shearing stress Consider a rectangular block of material subjected to shearing forces Sacting across two of its opposite faces (show in figure). The face I'm will move, relative distance And ma tondace NPr 10 MONG

MM! = MNXQ, where \$ is oduced of Shear the angle M 12 on Laipe L e i jui 1i) 10111105 Star \$2 pulle. Shoanny S X MM' The workdone = =  $\frac{1}{2} = \frac{1}{2} \times S \times M \times \phi$ tand = q, because , MM Very Small) S= IXLM, where I's Now, the shearing stress, and  $\phi = \frac{I}{2}$ 

(q = es = shear strain) Taking Unit depth normal to diagram, we have Strain energy = Workdone = TXLMXMNXE = IZ X Z X LM X MN Now (2 mx mn) is the Yolume of the rectangular block, of the rectangular block, since it has unit depth normal Strain energy; U= Z2 × Volumes \$ AMNP. This is the sharing stainenergy This is the sharing stainenergy for a block of material sub. to a for a block of material sub. to a Const. sharing stress throughout. 10721011

Strain energy in Torsion: Consider a Solid Géraldary 101 length L and radius Shaft of a torque Re, Subjected to 2 tuist O in the producing (Shown in Shaft the 1gure petre Romal Solid cirallar shaft workdore = # Tronchich is 2 that shaft as strain

But CO ritopy (or) θ 1 Kany e veli TH Where, T= Torque applied Ipor J= Polar moments of (.) G= Modulus of rigidity out = Length of the sheft, = Maximum, shear stress on the shaft on the surface 0= JIL R. W. and done = 1 × EXJ X EXI

X Workdone TR4 Now, XL .' Works <u>20)</u> X Workdo Volu rergy (07 ume Maria with hollow When shaf th and radius R Yac intern ain, Workdone = TO Ag ana

We have a 2 Z х 4) B K 1100 (Y, 2 Scanned with CamScanner

5.5) The external diameter of a hollow shaft is twice the internal diameter. It 13. Sub. to pure torque and it attains a maximum shear stress I. Show that the strain energy stored per unit volume of the shaft is 51. Such a shaft is required to transmit 5400 KW at 110 mm, with uniform torque, the max stress not exceeding 84 MM/m? Find: (1) The shaft diameter's its (ii) The energy stored per motion  $C = 90 \text{ GN}/\text{m}^{2}$ Take : RS Kidnike- -Stiven data: Golution: let R= External adius

of hollow shaft, and r= Internal radius of the hollow shaft = R/2 (Given). The General formula for energy (hollow shaft); strain  $U = \frac{T^2}{4c} \times \frac{(R^2 + r^2)}{\pi \pi} \times \frac{T}{\pi}$ Volume Volume  $\gamma =$ U/Volume 4 C M 5I K  $16CR^2$ Volume

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Volume Yower required to be transmitted P= 5400KW = 54×10 Wates Speed, N = mg 80/1 Max. Shear Stress, I= 84 MN/m2 Z= 84 × 10 N/m. (1) The Shaft diameter, D:-Now, P= 2TTNT 54×106 = 10 6900 = 468783 Nm too Also, -

27 T= = = XJ pt\_dt EX 32 11 4687 Ø.; 468783 P × I X 4687 4683 16 is 468 × 84×106 and Br 3× 10-6  $2^3 = 3032$ Scanned with CamScanner

0.312 m D= 3/2 mm  $d = \frac{7}{2} = \frac{312}{2} = \frac{312}{2}$ = 156mm. (i) Energy Stored per m? -X-(84 ×10) -X-90×109  $V/volume = \frac{5}{16} \frac{7}{16} = \frac{5}{16}$ U/volume = 24300F/m3 Hence, energy Stored perm<sup>3</sup> 1 = 24.5 KiJ/m3. 5.6) Compare the strain energies of the following two shafts sub. to the Same maximum shear stress in torsion:

(i) A hollow shaft having outer diameter "n" times the inner diameter. (ii) A Solid Shaft. Masses, lengths and materials of the two shafts are the same. let DH = Outer diameter of hollow shaft. the Solution: dH = Inner diameter of hollow shaft, and Ds = Diameter of Solid shaft. the \$ same mass: " mH= ms (Volume) + × J = (Volume) × Js Thur ,

It is given that, the material for solid and hollow Shafts Same. So,  $f_{g} = f_{H} = f.$ Length of \$ Solid and hollow Shafts shafts Same. So,  $l_s = l_H = L$ WKIT from D's Wolume) H X JH = (Volume) SSS = (D# - d#) XLXJ  $= \frac{\pi}{4} \mathcal{P}_{s} \times \mathcal{I} \times \mathcal{J}$  $= \frac{\pi}{4} \mathcal{P}_{s} \times \mathcal{I} \times \mathcal{J}$  $= \frac{\pi}{4} \mathcal{P}_{s} \times \mathcal{I} \times \mathcal{J}$ From the pom,

31  $\mathcal{D}_{\mathsf{H}}$ \_\_\_\_ 2dH Sub. 31  $d_{H}^{2} = \overline{a}$ ) S 2dH 2 n .2 ----- $(n^2-i)d$  $D^2$ Dit  $\frac{T^2}{X}$ Volum llow LH2) xL d# DH-C TXL Solid Scanned with CamScanne

 $\mathcal{D}_{H}^{+}$ -xJ I 4C hollow Solid 3×L Unollow d H Usolid Sub. in nt dH Uhollow 2 D5 )solid Ng n UHOlbow n d H Solid × UHollow Solid

 $(n^2 - 1)(n^2 + 1)$ Hollow  $n(n^2-1)$ Ugolid UHOllow Ann + Igoli d Therefore, hollow shaft is able strain absorb more to a Solid Shaft. as compared 1 to 2 for all shafts Ikollow "Conditions of the Usolid under proble m 110, external diameter of hollow shaft is in "times its transmits internal diameter. I Scanned with CamScanner

a torque. TH and develops Strain energy. UN. Another Solid Shaft has the Same external diameter as the hollow shaft and transmits torque T5 and develops a Strain energy Us. Find the Vatios UH and THE is the two shafts are to be Subjected to the Same max. Sheart stress. Assume the Shafts to be of the Same material and of the Same length Hence show that,  $\frac{T_H}{T_g} = \frac{U_H}{U_s}$ 

Solution! Let, DH = External diameter of the hollow shaft

: Internal diameter of 35 d# = the hollow shaft  $(\mathcal{P}_{H} = n d_{H}) -$ Ds = diameter of Solid Shaft Ds = DH = (Given) Hollow shaft, DHA-dH Now, For = 16 × 2 × For I, X IX Ds- $\frac{\pi}{16} \times \mathbb{Z} \times \left(\frac{\mathcal{P}_{H} + d_{H}}{-d_{H}}\right)$ T Scanned with CamScanner

Sub. H 7 H Ts Sub. -d# 4 ntdy T H nt. dH 4 n nt dH 15 1# TS DH+ dut WKT, × Volume

DH++dH4 Ex( )) 2) Pet al Π 2 X \$2 1 15 PH+-dH П × D.,2 I P LH 州 2 24 8 Sub. (1)

n=1)4 7-1 nª, dH 5a) & From  $H_{H} = H_{H}$ Strain energy due to Bending Figure shows a beam of Uniform Cross- section with Certain end Conditions such that the bending moment varies along 15 De length. Consider a Small length

dx of a beam where (39) the bending moments is M. Consider further a small strip EFGIH of thickness dy at a distance "y" from the neutral axis. Let "b" be the width of the strip. & Volume of the Strip 13 dx. dy b. Alle lenne here pill and + dy : strain energy of the Small Volume (dridy.b) = (stresson EFGH)2 × 10/ume

Small Volume Strain energy Xbxa ف ZEI<sup>2</sup> by<sup>2</sup>. dx. dy strain energy the within CC x 1.) 2 27 15 J 2118/17 TRA POURI

41 WKT, レーロボイン by dy = Sum of Second moments of areas bidy Jøydy = Moment of Inertia of Cross-Section = I Sub. 2 in M<sup>2</sup>dx dU = 2 E I 2  $= \frac{M^{-}}{DEI} dx$ dur The above expression gives the Strain energy of the beam of length dre ... : strain energy of the whole of the bearn of length doe

 $\int U = \int \frac{M^2}{2EI} dx - 3$ For any given load and end Conditions, M Can be expressed in terms of x and then the total strain energy Can be evaluated with help of eqn (3); In Case Mig Constant over the length, 1;  $U = \frac{M^2 L}{2EL}$ strain energy and deflection due to bending: R & alers profit In order to Calculate the deflection under the

load in the Cases of beams under the action of a Single point load, after Calculating the strain energy of beam, it is equated to the workdone by that bad for its gradual met movement equal to the deflection. If y is the deflection under the load wither, Unit from the the shearing (or) y = 24 (or) y = w W (5.8) A beam of length "L" simply supported at the ends is loaded with a point load Wat a distance "a" from one end. Et Assuming that the beam has

Constant Cross-section with moment of inertia as I and Young's modules of clasticity for the material of the beam as E, finds the Strain energy of the beam and hence find the deflection under the load. Strain energy due to Shearing may be neglected: Solution: Sale Ing I Ro = Way KA = Wb/L Scanned with CamScanne
reaction To find KB, take (#5 about A, moments (CCW=) +Ve) MA 0 5 = -Wa RB Wa RB = owwardward pward forces Gras W + RUB = =1-a - Wa Wa

any Section XX lying between For C; 02 Wb  $M_{x} =$ and for  $M_{x} = R_{B}(J)$ rgy stra UBC U= UAC  $\frac{1}{2ET}$  M<sup>2</sup> dx + Ŧ dx )dx  $\frac{1}{2EI} \times \frac{Wa}{12}$ 

 $\frac{W}{2EIJ^2}$ ٥ 多 Wat 六 2E1 α 0 C 2ET Wa 12 M. a ×-2 3 Wa 6 EIJ 11

 $\frac{Wa^2}{6FI^2}\left[(1-a)^2(1-a)\right]$  $\frac{Wa^2b^2}{x(1-a)}$ Wb2a3 GEI12 6EIL2 W222 62 ( a + (1 - a) $GEIL^2$  $W^2 a^2 b^2 l$ 6EIL<sup>2</sup>  $W^2 a^2 b^2$ Let Y' = Deflection Under load Workdone by the load W on the beam = - 1 W. y'

Since, the Workdone (49) = Strain energy  $\frac{1}{2}Wxy_c = \frac{Wa^2b^2}{6EIL}$  $\frac{y_{c}}{y_{c}} = \frac{Wa^{2}b^{2}}{3EJ}$ 5.9) For an expression for the Strain energy due to bending for a beam of length "1" Simply Supported at the ends and Carrying an uniformly distributed load w/ unit nen over whole of its span. The beam is of Constant Cross-Section throughout its length having =

EI. flexural rigidity as Solution Junit run Consider any Section XX at a distance "x" from the end A. The bending moment at the Section 18 given as

Wx · X Wi XX Mx = Wlx \_ 1xc  $\int \frac{M^2}{2ET}$ x /wl 2 x 1 2EI 2 wit A Day F  $x^3$ w.z 24

8EI D l 1 7 8 5  $\left( \right)$ 8EI 3 Е 5 2 8

w215 theorem: 2 orallotos Can be Castigliano's theorem used in the following Cases: 1) To determine the displacements of Complicated structures. 2. To find the deflection of beams Shearing (or) bending if the total strain energy due due\_ to shearing forces (an) bending moments (as the @ Case may be) 1111.62 . 17 W/ a 13 Known. 3. To find the defect deflections of Curved beams, springs etc.

Castigliono's theorem is stated as follows: 110 19 10 19 10 19 10 19 "If U is the total strain energy of any structure due to the application of external loads W1, W2, W3, .... Wn at points A,, A2, A3. An respectively in the direction AXI, AX2, AX3. AXA and due to Couples M, M2, ... Mn, at points B1; B2; B31. Bm respectively then the deflection at the points A, A2, A3, ..... An in the titections AX1, AX2, AX3 ... Axn are <u>av</u>, <u>av</u>, <u>av</u>, <u>av</u>, <u>av</u>, and the angular & positions of the Couples are du , du du du

and at the respective (5) and application " Points to remember while applying # Castigliano's theorem: (a) Treat, all the loads and Couples/moments as variables and Carry out partial differentiation. (b) Substitute the numerical Values of different bads and Couples in the above equation. 2. To findout the deflection (or) rotation at a point of the Structure where there is no bad (or) Couple acting, then it may be assumed that a dummy load W (or) dummy moment/Couple is

acting at that point an a value zero at the and give i.e.,  $\chi = \left(\frac{\partial U}{\partial W}\right)_{W=0}$  $=\left(\frac{\partial U}{\partial m}\right)m=0$ and 5.10) sing Castigliano's theorem the deflection under a obte Single Concentrated load applied to a Simply supported beam  $EI = 2.2 M Nm^2$ Shown gure.

W =,60KN ⓓ 1-304 0 RB Ra Č. ≤ MA = 0 (CCW =) +re) WX = 10 Đ  $R_B \times 4$ W= 60 KW 2: 1-> 0 to 3: Ma: BB 2 W Mx = WX RB ex Section XX at Consider a from B' distance 20  $R_B \times \mathcal{X} \rightarrow W(\mathcal{X}-3)$ r WX W/x

9 M Now x A W 4 /dx n ra 1-30 00 4-1 2 Scanned with CamScanner

 $S = \frac{W}{16EI} \int x^2 dx + \frac{W}{EI} \int \int \left(\frac{x - 4x + 12}{4}\right)^2$ (x=8x+16)  $x^2 dx$ W 16EF  $\frac{W}{16EI} \left[ \frac{x^3}{3} \right]^3 + \frac{9W}{16EI} \left[ \frac{x^3}{3} - \frac{8x^2}{2} \right]$ 16× - 28+16) TW . 16 16£ 50 × 103 0450 ·75X 2.2×10 1010110 Scanned with CamScanner

(5.11) In the figure, the Shown a Structure. Assuming the member to be of uniform @ Cross-Section throughout find the Strain energy stored by the structure and hence determine the Vertical deflection of end A. h Solution; Section AB; Scanned with CamScanne

 $M_{x} = W_{x}$ 61 63 UAB dx  $W^2 J^3$ Secti on 0 Ð UAB BC  $W^2 L^3$ 6EI

 $W^2 L^2$ 6EI the deflection be S Let A. Then, the by W = Total Strain end of Workdone Stores W 6E WL June -() you may . .